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THE
LINEAR
TABLES
DESCRIBED,
AND THEIR
UTILITY VERIFIED;
WITH
PRECEPTS AND EXAMPLES
FOR
SHORTENING CALCULATIONS
AND
PRESERVING ACCURACY,
IN THE
LUNAR METHOD
OF FINDING
LONGITUDE
AT SEA.

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P R E F A T O R Y

I N T R O D U C T I O N.

THIS Work contains two Methods of Computing the Longitude at Sea, having the Observed Distance of Sun and Moon or Moon and Star, the Observed Altitude of the Moon, and the Observed Altitude of the Sun or Star.

In the first of these Methods, the Effect of Refraction and Parallax is found, by the Application of a New Set of Linear Tables together with the Logarithms of Numbers, Sines, Tangents and Secants. In the second of these Methods, the Effect of Refraction and Parallax, is found, by working for the Angles at the Sun and Moon; and then the Effect whether it is additive to or subtractive from the Observed Distance, to get the true Distance of Centres.

In the first of these Methods, the Time at Greenwich is found in Hours, Minutes and Seconds; likewise, the Time at the Ship is found in Hours, Minutes and Seconds; and this compared with the Time at Greenwich gives the Longitude from Greenwich in Time, which is to be turned into Degrees and Minutes. In the second of these Methods, the Time at Greenwich is found in Degrees and Minutes; likewise, the Time at the Ship is found in Degrees and Minutes, and this compared with the Time at Greenwich gives the Longitude.

When the true Distance of Centres is found, by either of the Methods for that purpose; then, either of the Methods of finding the Times at Greenwich and at the Ship may be used, as it may be thought most convenient; and if a Watch be used for shewing either the Time at the Ship, or the Meridian for which it was set; it may be applied to the Time at Greenwich, and the Sum or Difference in the usual Manner will be the Longitude.

The first thing treated of in this Work, is the Doctrine of Refraction, in which it is shewn how to determine by Inspection, what the Refraction is at any Altitude, supposing the Refraction at the Horizon less than it is in Winter in the Northern Part of the Temperate Zone; this is of no small consequence in the Lunar Method of finding the Longitude at Sea; it is likewise of use in determining the Latitude.

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Then follows a Table shewing the Increase of the Moon's Semidiameter for Altitude, according to her respective Distances from the Earth, which are known from her Semidiameter and from her Horizontal Parallax; for, when either of these is small, the Distance is great, and *vice versa*.

Next it is shown how to find the Parallax in Altitude, either to the greatest Exactness by Calculation, or to the nearest Half-minute by a Table, or to a few Seconds of a Degree by Inspection, from a new Table for that purpose, the Construction of which has never before appeared.

In turning Time into Degrees and Minutes, it frequently happens that the Seconds of Time fall between the Minutes of Degrees, and thereby confound the Learner, this Difficulty is here removed by extending that part of the Table to Half-minutes of a Degree; and, as Longitude cannot properly exceed One Hundred and Eighty Degrees, either Easting or Westing, the remaining part of the Table is carried to that Number; there it stops, and what is to be done in the different Cases, is shewn by Examples.

The Dip of Horizon is another Subject of no small consequence in the Lunar Method of finding the Longitude at Sea; and the various allowances that have been made by different Writers, for this most necessary correction, make it indisputable, that many of them must have been erroneous. I have computed this Table from the most authentic Data, and applied it in a New manner to an interesting Subject; namely, the finding of Distances at Sea.

The Linear Tables described in this work, are upon a Plan which is entirely new, and which admits of Extension to a great variety of other Subjects, wherein Proportional Parts have been insuperable Hindrances to Calculators. It is a peculiar Circumstance attending the Construction of these Tables; that when Numbers are to be taken out by them, they require no Thought in the Calculator concerning Proportional Parts; which all other kinds of Tables require. In using other Tables, he must be ready at the Rule of Three Direct, with one, two or more Figures, sometimes several Times in a single Process, and frequently be perplexed in thinking whether their Results are to be added or subtracted.

The Linear Table I. is an Instance of the Utility of this Invention; for, if the same Table were expressed in a numerical manner, it would fill at least Twenty times the Space, without being of more real service in finding the Longitude. At the same time this Table shews by Inspection, what Data require attention to the smaller Parts of Degrees and what do not; this is not contained in any other Method whatever. If it be remarked that sometimes Index Three instead of Two may arise in using this Table, and that then four Figures for Seconds will come out for Number A; it may be observed, that this can happen at no other time but when one of the Altitudes

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Altitudes is very small, the other very great, and the Distance very small; and in such Cases, the Errors arising by the application of any other Table of this kind, adapted to one supposed Refraction at the Horizon, will be four times as great, as the Errors for want of the additional number in this Table.

A similar Remark may be made, on the application of Tables computed upon a supposed Equality of Refraction at the Horizon, at all Times and Places, with a certain Number of Minutes for the Horizontal Parallax. In the Formation of such Tables, the Effect of Refraction diminishes fast from the Horizon upward, but the Effect of Parallax diminishes slowly as the Cosine of the Altitude; and therefore, although Table I. is sufficient for the Correction of Refraction, it is by no means sufficient for the Correction of Parallax, because the latter will require four figures at least beside Index.

When a Table is formed for shewing the Effects of Refraction and Parallax at once, the Refraction near the Horizon in such a Table is suited to some particular place of the Earth, and the like is not to be expected at all other places; this is a part of the Foundation on which the Table stands, and when Pneumatic and Hydrostatic Instruments of a delicate kind are introduced to point out Corrections, it becomes a question how far those Substitutes may be depended on for answering the Purpose?

In the use of such a Table, formed for whole Degrees of Distance, and whole Degrees of Altitude for each Luminary, with a fixed Horizontal Parallax of the Moon; there will be at least four Corrections, generally occurring; namely, one for the intermediate Minutes of Distance, another for the Altitude of each Luminary, and a fourth for the Variation of Horizontal Parallax of the Moon, according to its difference from that which is supposed in the Table.

When these Corrections are making, some of them will be additive, others subtractive; some great, others small; all which tends to embarrass the Computor, nor can he with safety reject any of them, and instead thereof take the Tabular Result of whole Degrees; because the Corrections here are chiefly for the large Effect of Parallax (and not the small Effect of Refraction) which may amount to Nine Minutes of a Degree at Ten Degrees Altitude; Eight Minutes at Forty-two Degrees Altitude; and is so great as Two Minutes at Eighty Degrees Altitude. This appears at Sight by Linear Table XIV. It also appears that, with small Distances and small Altitudes of the Moon, the Error by using whole Degrees in such a Table, with its included Parallax, will frequently amount to more than Two Minutes of a Degree. It is therefore reasonable to conclude, that when such a Table is used without proportioning for the intermediate Minutes, under all the four forementioned circumstances, the Errors may (for want of them) amount to Ten Minutes of

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of a Degree, which at the Equinoctial is an Error of Three Hundred Nautical Miles.

Whilst the Method was practised, of finding Proportional Parts for the intermediate Numbers of Mr. Lyons's Table I. but a few out of a considerable Number of Persons, could understand it; this induced me to substitute the nearest whole Degrees, and the Twenty two Examples in this work, prove that no great Error in taking the Longitude at Sea, can have happened on that Account. The Table shewing the effects of Refraction and Parallax, requiring more and greater Corrections to be made, must therefore be with more and greater Difficulties accurately applied.

The Reductions into Seconds amongst the Linear Tables, will save the Computer both time and trouble, if he computes by the Sun and Moon's Angles; for in that Method, the Parallax in Altitude is had by Inspection from Table XIV. in Seconds, and the Refraction in Altitude is had in Seconds from Table VII. and with these, the Logarithms are taken out to get M. It is likewise ready for turning either the three hourly Differences, or the Difference between the first Hours and E, into Seconds by Inspection, in using the Formula for Longitude which is in this work.

The true Distance of Centres being found, the Times at Greenwich and at the Ship are found by the Instructions for that Purpose, and then the Longitude of the Ship.

Having enumerated the principal Steps that are to be taken in this Method, it seems not improper to deliver the first Principles upon which the Longitude at Sea depends, whether it be known from an Account of the Courses and Distances sailed, or discovered from actual Observations.

Geographers frequently name the whole Great Circle passing round the Earth from North to South, the Meridian of a place; but it seems more accurate to name it that Great Semi-circle passing through the place from Pole to Pole.

The Meridian of London passeth through St. Paul's Cathedral London. The Meridian of Greenwich passeth through the Royal Observatory at Greenwich.

The Meridian of London being continued northward, leaves England near Flamborough-head in Yorkshire. It then crosseth the Northern Seas, and being continued $38^{\circ} 29'$ from London, comes to the Earth's North Pole.

This Meridian being continued southward, leaves England near Brighthelmstone in Sussex. It then crosseth the British Channel and enters France near the Town of Auberville. By crossing the Pyrenean Mountains it enters Spain, and leaves it a little westward of the Entrance of Ebro River. It then passeth over the Mediterranean Sea, enters Africa near Oran and leaves it about 60 Miles eastward from Cape Three Points. It then enters the Ethiopian Sea and at
the

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the distance of $51^{\circ} 31'$ from London comes to the Equinoctial Line. Here the Longitude from London begins to be reckoned, in the Arch of a Great Circle which is every where equally distant from the Poles, Eastward to 180° . for East Longitude, and westward for West Longitude to 180° .

Continuing this Meridian 90° southward it comes to the South Pole of the Earth. This Extent from the North to the South Pole compleats the first Semi-circle of the Meridian of London, at all places of which, it is Noon Day at the same Instant.

Continue the first Semi-circle through the Earth's Poles to compleat the opposite or second Semi-circle, and it will pass through the Great South Sea, 180° at the Equinoctial distant from the first Semi-circle. At all places in this latter, it will be Midnight when it is Noon-day at the former. This compleats the Great Circle commonly called the Meridian of London, dividing the East Longitude from the West.

The nearest Distance from St. Paul's London to the Meridian of Greenwich is four Miles wanting a sixteenth of a Mile. The nearest Distance of those Meridians at the Equinoctial is six nautical Miles and a third. At the Equinoctial, a Degree of Distance is a Degree of Longitude, and a Mile of Distance is a Minute of Longitude.

Almost all Europe; Asia and Africa, are in East Longitude from London and Greenwich. North and South America are in West Longitude from Greenwich.

The Seas northward of Europe and Asia, the Baltic and Caspian Seas, almost all the Mediterranean, part of the Ethiopic Ocean, the Indian Ocean and part of the Pacific Ocean or Great South Sea, these are in East Longitude both from London and from Greenwich. The Atlantic or Western Ocean, and a great part of the Pacific Ocean, are in West Longitude from London and Greenwich.

Of all the things that can be either Objects perceivable by our Senses or Subjects for our Minds to contemplate on, there is scarce any thing more difficult to be defined, than what is commonly called Time.

The Idea which we commonly have of this Existence ariseth from a Comparison of one Moment or Instant with another, and according to the Length of Duration which we can perceive to be between them, the Quantity or Interval of Time between those Bounds is estimated.

According to these Principles, one might at first conclude that, when the Limits of two Intervals of Duration are at the same Distance from each other, the intermediate Times will be equal, or what amounts to the same thing, that Time flows uniformly; but this is contrary to the Principles whereby it is regulated.

The apparent Motions of the Celestial Bodies, and particularly of the Sun; these are the only Measures whereby the Quantities of Time

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Time are estimated, and they are sometimes nearly uniform, but most commonly to all appearance either accelerated or retarded.

When an Attempt of any kind is made for measuring the Quantities of Duration by Clocks, Watches or other Mechanical Contrivances, such are clogged with many and great Difficulties. 1st. They have no perfect Standard whereby they may be compared. 2^d. They are liable to various Degrees of Imperfection; the quantities of which (from them alone) can never be assigned. These Reasons, without mentioning any other, are sufficient to shew that they can be but Imitators of those accurate Measures whereby either equal or unequal Time is measured.

When the Centre of the Sun is apparently on the Meridian of Greenwich, the Solar Day begins there, and ends when that Centre is next apparently on that Meridian, which is the following Day at Noon.

Every Solar Day is either a little longer or shorter, than that going before or following it; this small Difference is called the Difference of the Equation of Time from one Day to another.

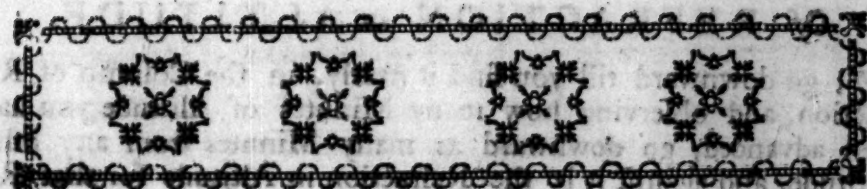
A Solar Day contains 24 Hours which are nearly equal to each other; each Hour is divided and subdivided into Minutes and Seconds of Time.

The greatest Difference between the Length of one Solar Day and another, is about the 20th of December, then it is Half a Minute of Time. Toward the Middle of February and May, the End of July and Beginning of November, this Difference amounts to but a few Seconds of Time.

The Circumference of the Equinoctial is 360° answering to 24 Hours, therefore Half a Minute of Time answers to Seven Minutes (or Miles) and half of a Degree of the Equinoctial. This is the greatest Error that can arise from the Extremes, by turning Solar Time into Degrees of the Equinoctial. In other Cases it will be less, and frequently so small as to be almost insensible. This is the Time which is used in the Lunar Method of finding Longitude at Sea.

By a Comparison of the true Distances of Centres, as deduced from the twenty-two Examples in this Work, it appears that the Methods of correcting Refraction and Parallax, both by the Linear Tables and by the Sun and Moon's Angles, are as accurate as other Methods that have been published; and that no censure can happen to me, for having substituted Mr. Lyons's whole Degrees, to take off the Computation of Proportional Parts; but when it is considered with what Ease they are practised and what Improvements they are capable of, they are both of the first Class for Truth and Utility.

Fleet-Street, **A. DUNN.**
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T H E
L I N E A R
T A B L E S
D E S C R I B E D, &c,

S E C T I O N I.

Of Refraction in Altitude, and the Tables which are formed
for shewing its Quantity.

REFRACTION in Altitude is either the number of Seconds, or Minutes and Seconds of a degree, which the Sun, Moon, Stars, or any other celestial Bodies appear more elevated above the Horizon of a Place, than they really are; and a Table of Refraction, is for shewing these Seconds or Minutes and Seconds of a Degree, from the Horizon to the Zenith. At the Horizon it is greatest, and at the Zenith it is nothing. In the North Temperate Zone, it hath been found near the Horizon, at one and the same place, Two Minutes of a degree greater in Winter than in Summer; from which the Medium has been taken to be Thirty Three Minutes. At the Horizon near the Equinoctial, it has been found Twenty Seven Minutes; and in the South Temperate Zone, it has been found greater than at the Equinoctial.

In the annexed Table, the Refraction at the Horizon is supposed 34'. 27" and against the different Altitudes are the correspondent Refractions in Altitude, supposing that the foresaid Refraction is at the Horizon. If the Refraction at the Horizon is less than 34'.

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27th; go downward till you find it nearly, in the Column of Refraction, and observing how many Minutes of Altitude you have then advanced, go downward as many Minutes from any other Altitude, and against it is the Refraction in Altitude for that Refraction at the Horizon.

In the Linear Tables, Article VII. is a Table of Refraction as it has been observed near London. In that Table, the Degrees and Parts of a Degree of Altitude run from left to right, and opposite to them are the Seconds of Refraction, with the Differences of Refraction in Seconds for each Degree. This Method of shewing the Refraction, is expeditious and certain to a Second of a Degree, and therefore well adapted for computation, where those Seconds are to be taken and subtracted from the Seconds of Parallax in Altitude.

From these Principles the two following Rules may be drawn and applied for finding the Refraction for any Altitude, and any Refraction at the Horizon less than that in a Table.

1st, When the Refraction at the Horizon is equal to that in a Table.

Subtract the correspondent Refraction in the Table, from the given Altitude, and the Remainder is that Altitude cleared from Refraction.

2^d, When the Refraction at the Horizon is less than that in a Table.

In the Column of Refraction, go downward to the given Refraction at the Horizon and note the Minutes of Altitude advanced. Then, advance as many Minutes in Altitude, from the Altitude given, and against it is the Refraction required.

EXAMPLE I.

Refrac. at Hor.	0°. 34'	27 th
Altitude observed	1. 0.	0
Refrac. for Alt.	0. 24.	32
Altitude cleared	0. 35.	28
This agrees with Sir Isaac Newton's Tables.		

EXAMPLE II.

Refrac. at Hor.	0°. 27'	0 th
Altitude observed	2. 0.	0
Refrac. for Alt.	0. 15.	30
Altitude cleared	1. 44.	30
This agrees nearly with Observations made near the Equinoctial.		

EXAMPLE III.

Refrac. at Hor.	0°. 31'	0 th
Altitude observed	3. 0.	0
Refrac. for Alt.	0. 13.	26
Altitude cleared	2. 46.	34
This agrees nearly with a Medium between Sir Isaac Newton and Dr. Brook Taylor.		

EXAMPLE IV.

Refrac. at Hor.	0°. 32'	0 th
Altitude observed	4. 0.	0
Refrac. for Altitude	0. 11.	16
Altitude cleared	3. 48.	44
This agrees nearly with a medium between Sir Isaac Newton and Dr. Bradley.		

EXAMPLE V.

Refrac. at Hor.	0°. 33'	0 th
Altitude observed	5. 0.	0
Refrac. for Alt.	0. 9.	28
Altitude cleared	4. 50.	32
This agrees nearly with a medium between Sir Isaac Newton and Dr. Bradley		

EXAMPLE VI.

Refrac. at Hor.	0°. 33'	30 th
Altitude observed	6. 0.	0
Refrac. for Alt.	0. 8.	10
Altitude cleared	5. 51.	50
This agrees nearly with a medium between Dr. Halley, Dr. Bradley, and M. de la Caille.		

Of

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S's Horizontal Parallax.										S's Parallax in Altitude.									
54'	55'	56'	57'	58'	59'	60'	61'	62'		54'	55'	56'	57'	58'	59'	60'	61'	62'	
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	
2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	
3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	
4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	
5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	
6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	
7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	
8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	
9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	
10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	
11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	
12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	
13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	
14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	
15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	
16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	
17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	
18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	
20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	
22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	
23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	
24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	
25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	
26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	
27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	
28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	
29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	

S's Horizontal Parallax.										S's Parallax in Altitude.									
54'	55'	56'	57'	58'	59'	60'	61'	62'		54'	55'	56'	57'	58'	59'	60'	61'	62'	
30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	
31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	
32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	
33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	
34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	
35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	
36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	
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40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	
42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	
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44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	
45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	
46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	
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49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	
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53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	
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66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	
67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	
68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	
69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	
70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	
71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	
72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	
73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	
74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	
75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	
76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	
77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	
78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	
79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	
80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	
82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	
83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	
84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	
85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	
86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	
87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	
88	89	90																	

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X

X

Of the MOON'S SEMIDIAMETER. 3

SECTION II.

A Table shewing the Increase of the Moon's Semidiameter, for her greatest, mean and least Distances from the Earth; and for every Five Degrees of Altitude.

Moon's Alt.	Moon's great. Dist.	Moon's mean Dist.	Moon's least Dist.
D.	"	"	"
0	0	0	0
5	1	1	2
10	2	3	3
15	3	4	5
20	5	3	6
25	6	7	8
30	7	8	9
35	8	9	11
40	9	10	12
45	10	11	13
50	11	12	14
55	11	13	15
60	12	14	16
65	13	14	17
70	13	15	18
75	13	15	18
80	14	16	18
85	14	16	19
90	14	16	19

EXAMPLE I.

Observed Alt.	10°.	15'.	0".
Hor. Semidiam.	0	14	44
Seconds for Alt.	0	0	3
true Semidiam.	0	14	47

EXAMPLE II.

Observed Alt.	40°.	0'.	0".
Hor. Semidiam.	0	16	8
Seconds for Alt.	0	0	10
true Semidiam.	0	16	18

EXAMPLE III.

Observed Alt.	80°.	0'.	0".
Hor. Semidiam.	0	16	42
Seconds for Alt.	0	0	18
true Semidiam.	80	17	0

SECTION III.

Of the Moon's Horizontal Parallax, and Parallax in Altitude.

The Moon's Horizontal Parallax, is the Angle made by two straight lines, drawn from the Centre of the Moon, one to the Centre of the Earth, the other to its Surface. Thus the Horizontal Parallax is understood whether the Moon is in the Horizon or not; but, it will at all times be in the Horizon of some Place, of the Earth or Sea. Consequently, the nearer the Moon is to the Earth, the greater is her Horizontal Parallax; and, there is the same Horizontal Parallax, whether the Moon is in the Horizon, the Zenith, or between the Horizon and Zenith, whilst her Distance from the Earth is the same.

The Moon's Parallax in Altitude, is the Difference between the Altitude of the Moon as seen from the Surface of the Earth or Sea, and the Altitude which the Moon would have at the same time, if viewed from the Earth's Centre, and elevated above an Horizon a

4 Of the MOON'S PARALLAX in ALTITUDE.

Semidiameter of the Earth lower than that of its Surface. Consequently, the Moon's Parallax in Altitude is greatest near the Horizon; it decreaseth toward the Zenith, and in the Zenith it is nothing.

By the like Reasoning, the Moon's Semidiameter is least near the Horizon and greatest in the Zenith; at her greatest, mean and least Distances from the Earth.

At any given Altitude of the Moon, it is thus;
As the Radius or Sine of 90 Degrees,
Is to the Cosine of the Moon's Altitude observed;
So is the Horizontal Parallax, in Seconds of a Degree,
To the Parallax in Altitude, in Seconds of a Degree.

The Moon's Parallax in Altitude, added to the observed Altitude, clears the Altitude from Parallax in Altitude.

Annexed, is a Table shewing the Moon's Parallax in Altitude, for every Degree of Altitude, and every Minute of Horizontal Parallax, to the nearest Half Minute of Parallax in Altitude. In this Table, the Figure in Tens place upward, is supposed to be prefixed to each of the Figures under it.

In the Linear Tables, Article XIV, is a Table shewing the Parallax in Altitude for any Horizontal Parallax, and given Altitude, to the Exactness of a few Seconds, by Inspection. The use of this Table, is as follows.

Find the Moon's Altitude in the uppermost Line, and from it guide your eye slope-way from Right to Left downward, till you come to the Horizontal Parallax among the Horizontal Lines, and perpendicularly under this, is the Parallax in Altitude, in Minutes and Parts of a Minute, or in Seconds. Note, that the distance between one Perpendicular Line and another is 60". By this Method, the Parallax in Altitude may be found, to less than 15" instantly by Inspection; but, if greater Accuracy be required, with a pair of Compasses do thus,

From the Lowermost Line open the Compasses upward to the Horizontal Parallax, with which Extent remove to the slope of Altitude. Then, take the nearest Distance to the next Right-hand Perpendicular for additional Seconds, and measure them by the Scale at the left End. These added to the Seconds under the said Perpendicular, give the Parallax in Seconds, or in Minutes and Seconds.

This Method is not only expeditious but may be depended on to a few Seconds, and therefore may be of use in many Cases, where the greatest Accuracy is not wanted.

III. By CALCULATION.

EXAMPLE I

Moon's Alt. $34^{\circ} 16' 0''$ Log. 9.9172
3560" Hor. Par. 0 $59' 20''$ Log. 3.5514
2942" Par. Alt. 0 $49' 2''$ Log. 3.4686

EXAMPLE II.

Moon's Alt. $76^{\circ} 48' 0''$ Log. 9.3586
3280" Hor. Par. 0 $54' 40''$ Log. 3.5169
749" Par. Alt. 0 $12' 29''$ Log. 2.8743

Of the MOON'S PARALLAX in ALTITUDE. 5

In the two foregoing Examples, Radius is rejected in the Total of the Logarithms which are added together, to get the Logarithm of the Parallax in Altitude.

2d, By CALCULATION and INSPECTION.

Examples.	Alt. of Moon.		Moon's Hor. Par.		Moon's Par. Alt.	Moon's Par. Alt.	Diff. by Inspection.
	° ' "		" "		" "	" "	" "
1	55.56	—	60. 5	—	33.40	or 2020	— 3
2	18.56	—	55.30	—	52.30	or 3150	— 5
3	27. 2	—	59.58	—	53.26	or 3206	— 4
4	9.38	—	54.42	—	53.56	or 3236	— 5
5	49.57	—	57. 8	—	36.46	or 2206	— 4
6	47.42	—	57. 6	—	38.26	or 2306	— 1
7	30. 0	—	60. 0	—	51.58	or 3118	— 3
8	20. 9	—	57.24	—	53.54	or 3234	— 3
9	21.26	—	56.30	—	52.36	or 3156	— 5
10	15.21	—	60.25	—	58.16	or 3496	— 1
11	43.20	—	58.50	—	42.48	or 2568	— 3
12	20.34	—	56.24	—	52.48	or 3168	— 4
13	27.30	—	57. 3	—	50.36	or 3036	— 5
14	64.30	—	55.29	—	23.53	or 1433	— 0

By the above Examples, it appears that from this Table, the Parallax in Altitude may be taken without an Error of Six Seconds from the Truth; for the above Differences are all of one kind; and this may be of Use on many occasions when that Parallax is not wanted nearer the Truth, and even in many cases concerning the Longitude at Sea, as that Error alone would produce but an Error of Three Nautical Miles at the Equinoctial and Two coming into the British Channel.

Seeing that this Method of finding the Parallax in Altitude by Inspection is so accurate, it is applicable on several important occasions. In taking the Latitude by the Moon's observed Meridian Altitude, it clears that Altitude from Parallax in Altitude, to any desired Accuracy, with ease and certainty. The like for Altitudes of the Moon out the Meridian, in order to find the Latitude, Longitude, Azimuth and Time, from cotemporary Observations; for in either of these cases, the Refraction is subtractive and the Parallax in Altitude additive, and from both of these the true Altitude is found. It is farther of great utility in finding the exact quantity of Refraction in Altitude near the Horizon in different Climates (a matter of the greatest consequence in taking the Longitude at Sea, as mentioned in my Treatise on that Subject) and farther, it is applicable with Facility, for finding the Deviation of the Spheroidal Horizon from that which would be formed on a Spherical Earth. Many other Uses of this Table might be mentioned.

6 A TABLE of DEGREES and TIME.

D. H. M. M. M. S.	D. H. M. M. M. S.	D. H. M. M. M. S.	D. H. M. M. M. S.
0½—0. 2	15½—1. 2	30½—2. 2	45½—3. 2
1 —0. 4	16 —1. 4	31 —2. 4	46 —3. 4
1½—0. 6	16½—1. 6	31½—2. 6	46½—3. 6
2 —0. 8	17 —1. 8	32 —2. 8	47 —3. 8
2½—0.10	17½—1.10	32½—2.10	47½—3.10
3 —0.12	18 —1.12	33 —2.12	48 —3.12
3½—0.14	18½—1.14	33½—2.14	48½—3.14
4 —0.16	19 —1.16	34 —2.16	49 —3.16
4½—0.18	19½—1.18	34½—2.18	49½—3.18
5 —0.20	20 —1.20	35 —2.20	50 —3.20
5½—0.22	20½—1.22	35½—2.22	50½—3.22
6 —0.24	21 —1.24	36 —2.24	51 —3.24
6½—0.26	21½—1.26	36½—2.26	51½—3.26
7 —0.28	22 —1.28	37 —2.28	52 —3.28
7½—0.30	22½—1.30	37½—2.30	52½—3.30
8 —0.32	23 —1.32	38 —2.32	53 —3.32
8½—0.34	23½—1.34	38½—2.34	53½—3.34
9 —0.36	24 —1.36	39 —2.36	54 —3.36
9½—0.38	24½—1.38	39½—2.38	54½—3.38
10 —0.40	25 —1.40	40 —2.40	55 —3.40
10½—0.42	25½—1.42	40½—2.42	55½—3.42
11 —0.44	26 —1.44	41 —2.44	56 —3.44
11½—0.46	26½—1.46	41½—2.46	56½—3.46
12 —0.48	27 —1.48	42 —2.48	57 —3.48
12½—0.50	27½—1.50	42½—2.50	57½—3.50
13 —0.52	28 —1.52	43 —2.52	58 —3.52
13½—0.54	28½—1.54	43½—2.54	58½—3.54
14 —0.56	29 —1.56	44 —2.56	59 —3.56
14½—0.58	29½—1.58	44½—2.58	59½—3.58
15 —1. 0	30 —2. 0	45 —3. 0	60 —4. 0

SECTION IV.

In this Table, each Degree is four Minutes of Time, and each Minute of a Degree is four Seconds of Time. An Hour of Time is fifteen Degrees, and a Minute of Time is fifteen Minutes of a Degree.

When either the Degrees or the Minutes of a Degree do not exceed Sixty, the Time is opposite to them in the First part of the Table. Consequently, when the Time doth not exceed four Hours, the Degrees are opposite thereto; and when the Time doth not exceed four Minutes, the Minutes are opposite thereto, to the nearest half Minute, in the same part of the Table.

When the Degrees are between Sixty and One Hundred and Eighty, the Hours and Minutes are opposite to them in the Second part of the Table. When the Degrees exceed One Hundred and Eighty, the Excess must be found by Subtraction and against the Remainder

A TABLE of DEGREES and TIME. 7

D. H. M.	D. H. M.	D. H. M.	D. H. M.
61—4. 4	91—6. 4	121—8. 4	151—10. 4
62—4. 8	92—6. 8	122—8. 8	152—10. 8
63—4. 12	93—6. 12	123—8. 12	153—10. 12
64—4. 16	94—6. 16	124—8. 16	154—10. 16
65—4. 20	95—6. 20	125—8. 20	155—10. 20
66—4. 24	96—6. 24	126—8. 24	156—10. 24
67—4. 28	97—6. 28	127—8. 28	157—10. 28
68—4. 32	98—6. 32	128—8. 32	158—10. 32
69—4. 36	99—6. 36	129—8. 36	159—10. 36
70—4. 40	100—6. 40	130—8. 40	160—10. 40
71—4. 44	101—6. 44	131—8. 44	161—10. 44
72—4. 48	102—6. 48	132—8. 48	162—10. 48
73—4. 52	103—6. 52	133—8. 52	163—10. 52
74—4. 56	104—6. 56	134—8. 56	164—10. 56
75—5. 0	105—7. 0	135—9. 0	165—11. 0
76—5. 4	106—7. 4	136—9. 4	166—11. 4
77—5. 8	107—7. 8	137—9. 8	167—11. 8
78—5. 12	108—7. 12	138—9. 12	168—11. 12
79—5. 16	109—7. 16	139—9. 16	169—11. 16
80—5. 20	110—7. 20	140—9. 20	170—11. 20
81—5. 24	111—7. 24	141—9. 24	171—11. 24
82—5. 28	112—7. 28	142—9. 28	172—11. 28
83—5. 32	113—7. 32	143—9. 32	173—11. 32
84—5. 36	114—7. 36	144—9. 36	174—11. 36
85—5. 40	115—7. 40	145—9. 40	175—11. 40
86—5. 44	116—7. 44	146—9. 44	176—11. 44
87—5. 48	117—7. 48	147—9. 48	177—11. 48
88—5. 52	118—7. 52	148—9. 52	178—11. 52
89—5. 56	119—7. 56	149—9. 56	179—11. 56
90—6. 0	120—8. 0	150—10. 0	180—12. 0

Remainder are the Hours and Minutes in one of the parts of the Table, which being added to Twelve Hours gives the Time required.

The Reverse, gives the Degrees and Minutes, to the nearest Half Minute of a Degree.

EXAMPLE I.

°	'	is	H	'	"
67	24½	is	4	29	38
for 67	0	=	4	28	0
	24½	=		1	38

EXAMPLE III.

°	'	is	H	'	"
236	18½	is	15	45	14
for 180	0	=	12	0	0
	56	=		3	44
	18½	=		1	14

EXAMPLE II.

°	'	is	H	'	"
163	40½	is	10	54	48
for 163	0	=	10	52	0
	40	=		2	48

EXAMPLE IV.

H	'	"	is	°	'
19	47	26	is	296	51½
for 12	0	0	=	180	0
	7	44	=		116
	3	26	=		51½

A New

Of the DIP of HORIZON.

A New Table shewing the Dip of Horizon to 600 Feet above the Surface of the Sea; with its Use in determining the Horizontal Distances of Objects.

Feet.	Dip.	Feet.	Dip.	Feet.	Dip.	Feet.	Dip.
' "	' "	' "	' "	' "	' "	' "	' "
0—0.0	25—5.18	55—7.53	180—14.15	310—18.41			
1—1.4	26—5.25	60—8.14	185—14.26	320—18.59			
2—1.30	27—5.31	65—8.34	190—14.38	330—19.17			
3—1.50	28—5.37	70—8.53	195—14.50	340—19.54			
4—2.7	29—5.43	75—9.12	200—15.1	350—19.52			
5—2.23	30—5.49	80—9.30	205—15.12	360—20.8			
6—2.36	31—5.55	85—9.47	210—15.23	370—20.25			
7—2.49	32—6.1	90—10.4	215—15.34	380—20.41			
8—3.0	33—6.6	95—10.21	220—15.44	390—20.58			
9—3.11	34—6.11	100—10.37	225—15.55	400—21.14			
10—3.22	35—6.17	105—10.53	230—16.6	410—21.30			
11—3.31	36—6.22	110—11.8	235—16.17	420—21.45			
12—3.41	37—6.27	115—11.23	240—16.27	430—22.1			
13—3.50	38—6.32	120—11.38	245—16.37	440—22.16			
14—3.58	39—6.37	125—11.52	250—16.47	450—23.1			
15—4.7	40—6.43	130—12.6	255—16.57	500—23.45			
16—4.14	41—6.48	135—12.20	260—17.7	510—23.59			
17—4.23	42—6.53	140—12.34	265—17.17	520—24.13			
18—4.30	43—6.58	145—12.47	270—17.27	530—24.26			
19—4.38	44—7.3	150—13.0	275—17.37	540—24.40			
20—4.45	45—7.8	155—13.13	280—17.46	550—24.54			
21—4.52	46—7.12	160—13.26	285—17.55	560—25.7			
22—4.58	47—7.17	165—13.38	290—18.5	570—25.21			
23—5.5	48—7.21	170—13.50	295—18.14	580—25.34			
24—5.12	49—7.26	175—14.3	300—18.23	590—25.47			
25—5.18	50—7.30	180—14.15	305—18.32	600—26.0			

The Height to which this Table is carried above the Surface of the Sea, is sufficient for all cases wherein the Dip is wanted to be known in order to clear the observed Altitude of either Sun, Moon or Star. It is calculated anew from proper Data. At the Height of a Ship's Deck, it gives the Dip Half a Minute of a Degree more than some, and less than others, who have been esteemed our best Writers on this Subject. Whilst such Uncertainties have been concerning the Quantity of Dip, Corrections of the observed Altitudes to Seconds of a Degree, must have been needless.

SECTION

Of the DIP of HORIZON.

SECTION V.

Of the Dip or Depression of the Apparent Horizon, below the Horizon of the Sea.

When the Eye of an Observer is either in or supposed to be in the Surface of the Sea; the Celestial Bodies appearing to coincide with the Surface of the Sea, are said to be in the true Horizon of the Sea at that Place; but if the Eye be above the Surface of the Sea, the same Bodies at the same time appear Elevated a certain number of Seconds, or Minutes and Seconds of a Degree. This Elevation is called the Dip of Horizon, and is to be subtracted from the observed Altitude, to clear it therefrom.

A Table shewing the Dip of Horizon having the Height of the Eye above the Surface of the Sea, is made, by having the Diameter of the Earth in Feet, and the Height of the Eye in Feet. If the former of these is not near the Truth, the Table will not be quite correct. I have computed the annexed Table, from the latest Discoveries concerning the Dimensions of the Earth's Diameter.

The first part of this Table, will answer for all the usual cases, when Altitudes have been taken in any part of a Ship at Sea; the second part will be of use for ascertaining Distances of places from the Ship.

In this Table, sixty second make a Minute or Nautical Mile, and the Nautical Mile is to the English Mile, as 60 to 70 nearly; therefore, when the Nautical Miles are found, take its Sixth part and add it to them, this gives the English Miles nearly.

The Alteration of the Position of the Horizon of a Place, is a Minute of a Degree in each Nautical Mile; therefore, the Dip of Horizon being accurately known, the Distance is also known as in the following Examples.

EXAMPLE I.			
Height 24 Feet			
Altitude observed	32°.	30'	0".
Dip of Horizon	0.	6	3.
Altitude cleared	32	23	57.

EXAMPLE III.			
Height 150 Feet			
Farthest Surface at Sea	0°.	13'	0".
Nautical Miles		13	miles.
English Miles		15½	miles.

EXAMPLE V.			
Height of a Light House		600 Feet.	
Its Light horizontal at Sea.			
Distance in N. Miles	26	Miles.	
E. Miles	30½	Miles.	

EXAMPLE VII.			
Height of one Hill	500 Feet.		
Height of another Hill	450 Feet.		
Dip for both Heights	46'	46".	
Distance in N. Miles	46½	Miles.	
Distance in E. Miles	54½	Miles.	
When ½ Heights appear in the Horizon.			

EXAMPLE II.			
Height 120 Feet.			
Altitude observed	25°.	15'	0".
Dip of Horizon	0.	5	20.
Altitude cleared	25.	9	40.

EXAMPLE IV.			
Height of a Ship's Deck		60 Feet.	
Height of another's Deck		50 Feet.	
Dip for first Ship		8'	14".
Dip for second Ship		7'	30
Ships Distance apart	13.	44	
Nautical Miles		15½	miles.
English Miles		18½	miles.

EXAMPLE VI.			
Height of a Hill	800 Feet.		
Height of a Mast	100 Feet.		
Dip for the Hill	23'	45".	
Dip for the Mast	10'	37".	
Dip for both	34.	22".	
Make Nautical Miles	34½	miles.	
And English Miles	40	miles.	
Distance when their Tops in the Horizon.			

C

SECTION

SECTION VI.

Of LARGE TABLE I. in the Linear Table.

This Table has three Lines; 1st. Lines drawn from the Left hand toward the Right, beginning at 4° and ending at 50° . In some part or other of these, the Lesser Altitude of Sun, Moon or Star, is found in computing the Longitude. 2d. Lines drawn perpendicular to and crossing the former, beginning at 8° , and ending at 90° . In some part or other of these, the Greater Altitude is found. 3d. Lines crossing the two former, and numbered with Index 2. and three Figures following it.

When a Number is to be found by this Table, the lesser and greater Altitudes are to be found as before directed, and in the Angle of meeting is the Number sought, amongst the third sort of Lines beforementioned.

The best Observations that has been made in different Climates, prove that at the Altitude of a few Degrees, the Refraction may be too imperfectly known, for a desired Determination of the Longitude by the Lunar Method. There are proofs of such uncertainty, as high as eight or ten Degrees of Altitude; this renders lesser Altitudes of less consequence, and shews that the success is chiefly to be expected from greater Altitudes.

When the Point is found where the Lines of lesser and greater Altitude meet in this Table, it is to be observed that, near that Point, the Distance between two Lines of the third sort contains ten Units, and as many of these as that Point is past the foregoing Line, being added to its Number, gives the Number required.

In taking out the Number from this Table, there is no particular Nicety required, but what the Eye can immediately discern and the Judgment determine, except when one of the Altitudes is very near the Horizon; and then, the Error may be greater through the uncertainty concerning Refraction, than that of applying this Table.

When the Number is thus found, it is to be worked as the Formula directs, until Number A is found.

When the two Lines of Direction from the Lesser and greater Altitude, do not fall within this Table but without it, neither this Table, nor Table II. following it are to be applied, but Table III. as is directed in the Use of that Table farther on.

In using this Table I. the Number may be taken out in usual cases, to the nearest Quarter of a Degree for both the lesser and greater Altitude, and in some cases to twice that number of times if not more, without ever needing Proportional Parts for any place in the Table; which is a great Advantage over the Numerical Method of Expression.

This Table is illustrated, in finding the Correction for Refraction, in the Examples farther on.

SECTION

LONGITUDE Instructions; By S. Durrant, Esq.

1. Get the Altitude of the Sun's Centre cleared from Dip & Semidiameter, the Altitude of the Moon's Centre cleared from Dip & Semidiameter, & the Sun- & Moon's nearest Limbs. Add 32 to the observed Distance of Limbs to get the Rough Central Distance, with this from Ephemeris page 8, 9, 10 or 11 for the Month, where the Day of the Month & Sun are together take out the nearest Hour; this is the rough Hour for Greenwich.

2. The Ephemeris has the
 Sun's true Semidiameter page . . . 3.
 Moon's true Semidiameter 7.
 Moon's Horizontal Parallax 7.
 Three hourly Distances 8, 9, 10, 11.
 Sun's true Declination 2.

The Requisite Tables have the
 Seconds for Moon's Altitude . . . page . 153.
 Refraction in Altitude 2.
 Moon's Parallax in Altitude . . . 3, 4, 5.
 Time & Degrees 6.

3. Begin the Formula with the Rough Central Distance & Rough Hour for Greenwich, & go on as it directs until you come to the Number E in it. Then, in usual Cases, the nearer the Rough Central Distance in Degrees, comes to 120° , the greater it is; & the nearer it comes to 20° , the less it is. A great Altitude of the Moon may be that above 20° . When the Rough Central Distance in Degrees is great, & especially, when the Moon's Altitude is also great; then Number E may be written for the true Distance of Centres.

4. For small Distances, or small Moon's Altitude, Take the Moon's Parallax in Altitude from Requisite Tables page 3, 4, 5; with this & the Distance take the Seconds from large Table IV. Also with Number C & the Distance, take the Seconds from the same Table IV; & the Difference of these Seconds is F.

5. From amongst the three hourly Distances in Ephemeris page 8, 9, 10 or 11; take two such Distances following each other, so that the true Distance of the Centres falls between them; then go on by the Formula till you have the Time at Greenwich; this is past noon for Greenwich.

6. From Ephemeris page 2. take the Sun's true Declination for the Hour at Greenwich; & when the Declination & Latitude are both North or both South, subtract the Declination from 90° ; but in other Cases, add the Declination to 90° , to get the Polar distance. And subtract the Sun's Co-altitude from the Half sum to get a Remainder. Then go on by the Formula, till you have the Time at the Ship; this will be past Noon at the Ship in an Afternoon Observation, & short of noon in a Forenoon Observation.

7. In an Afternoon Observation, subtract one Time from the other, the Remainder is the Longitude; & it is West Longitude when the Time at Greenwich is greatest, but otherwise East Longitude. In a Forenoon Observation, add the two Times together, the Sum is the Longitude West, & it's Remainder to either 24 Hours or 360, is East Longitude. NB. These general Receipts, in several Parts of the Operation, may be shortened, by attending to the following Directions mentioning each in particular.

Published according to Act of Parliament May 29th 1782 by Samuel Durrant, Printer to the Admiralty.

THE HISTORY OF THE UNITED STATES

The history of the United States is a story of growth and development. It begins with the first settlers who came to the Americas in search of a new life. These early pioneers faced many challenges, but they persevered and built a new society. Over time, the United States grew from a small colony into a powerful nation. It fought wars, both with and without, and emerged as a global leader. The story of the United States is one of resilience and achievement. It is a story that continues to inspire and inform us today.

Supplementary LONGITUDE Instructions; By S. Dunn.

Of Preparations.

1. When the Sun & Moon's nearest Limbs have been observed; add 32' to get the Rough Central Distance. Also, add the Sun & Moon's true Semidiameters, & Seconds for Moon's Altitude; to get L.
2. When the Star & Moon's nearest Limb have been observed; add 16' to get the Rough Central Distance. Also add the Moon's true Semidiameter, & Seconds for Moon's Altitude, to get L.
3. When the Star & Moon's farthest Limb have been observed; subtract 16' to get the Rough Central Distance. Also, subtract the Moon's true Semidiameter, & Seconds for Moon's Altitude, to get L.

Of Contractions.

1. In taking out the Number from large Table I, the nearest whole Degrees may be used in the most usual Cases.
2. When the Number falls above or near the Crooked Line in large Table I, you need not find the Numbers A, B; but take from large Table III, the Seconds that are to be added to Number L, to give Number D.
3. When the Sun or Moon's Altitude is very small, the Refraction should be taken from the Altitude, before it is written in the Formula, next after the Horizontal Parallax.
4. In computing the Time at the Ship; the third Number or Sun's Co-altitude, is that of the Altitude lessened both by Dip & Refraction.

Of Operations.

1. The Observations should not be made when the Sun or Moon are very near the Horizon. If the Moon is very near the Horizon, Proportional Parts should be used in large Table I.
2. Four Places of Logarithms with Index, are used, till the last Cosine; then the fifth Figure is 5 when 1 remains, & 0 when 0 remains.
3. C must not be added to D, unless the 1st Arc is least of the two Arcs, & at the same time D is less than 90°. In other Cases, subtract C from D.

Of Observations.

1. In observing for Longitude only, without use of a Watch, the Sun should not be very near the Meridian; then Observations will determine Latitude. Also, when the Moon is near the Meridian, Observations will determine Latitude.
2. When the Sun is far à Meridian & not near the Horizon, Observations are best for the Time & setting a Watch.
3. In the Night, the Watch shows Time at the Ship. When no Watch is used in the Night, the Right Ascension of Sun & Star, compared with the Star's distance from the Meridian, either past or short of it, gives Time at the Ship. In this, the Chart of Zodiacal Stars is useful.
4. The Stars of first Magnitude out of the Zodiac, are useful for Time at the Ship; such as Capella, the principal in Orion, Canopus, Sirius, Procyon, Lyra. And so may Venus, Mars, Jupiter & Saturn.
5. The same Stars & Planets may be used for Latitude by Meridian Altitudes, Elapsed Time, & otherwise.

6. The principal Stars used in the Lunar Method are, Aldebaran, Pollux, Regulus, Spica, Antares, Aquila, Fomalhaut. The others are, Capella, Orion's Sirius, Procyon, Canopus, Arcturus, Lyra; the Bears, Ship & Cross.

Published according to Act of Parliament May 29th 1782 by Samuel Dunn, Fleet Street London.

2nd January 1900

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Of the LINEAR TABLES.

11

SECTION VII.

OF LARGE TABLE II. in the Linear Tables.

In this Table, L is the observed Distance of Centres, and B the Number of Seconds to be taken out, and added to or subtracted from A. In doing this, if L be near 90 Degrees, it is to be found to the nearest Half Degree; but if it be near the Middle of the Quadrant, it should be taken to the nearest Quarter of a Degree; and if it be toward the Beginning of the Quadrant, as from 20 to 15 and 10 Degree, it should be taken to the nearest Half-quarter of a Degree; and opposite thereto is the Number B in Seconds, which are to be added to, or subtracted from A, as denoted at the Top of the Table, to give the Correction additive to L to give D.

This Table is illustrated, in finding the Correction for Refraction, in the Examples farther on.

SECTION VIII.

OF LARGE TABLE III. in the Linear Tables.

This Table is to be used when Large Table I. will answer to no Number by the Intersection of Lines within it. As in large Table II. so here, L is to be taken to either Half or Quarter or Half a Quarter of a Degree; and against it is the Number of Seconds and part of a Second (which are here called B) and are to be added to L to give D.

This Table is illustrated, in finding the Correction for Refraction in the Examples farther on.

SECTION IX.

OF LARGE TABLE IV. in the Linear Tables.

When the Observed Distance of Centres hath been cleared from Refraction and Parallax, by either of the Methods treated of in the *Theory and Practice of Longitude at Sea*, or that by either of the two Formulas in this Treatise; there is a small Correction to be farther made, for small Distances and small Altitudes of the Moon, which is most easily done by this Table.

This Table hath three different Sorts of Lines; 1st. Perpendicular lines leading from the Numbers 10°. 20°. &c. to 90° and returning again to 120° in some Part of these, the Distance L or rather E is found. 2d. Parallel Lines drawn from left to right, from the Numbers 10'. 22'. &c. to 62'. in some Part of these, the Moon's Parallax in Altitude is found. 3d. Lines which are partly curved, drawn across the Table; amongst these latter (as in large Table 1.) is the last Correction F expressed in Seconds at the End of the

C 2

Lines,

Of the LINEAR TABLES.

Lines, when the Correction C is found as a Parallax in Altitude, and E as a Distance, and the Angle of their Meeting falls without the Table; but when these meet within the Table, the Number found by the Curve lines must be taken from that Correction and the Remainder is F.

As Table I. is expressive of Answers to any Part of a Degree for both Altitudes, so is this Table IV. to any Part of a Minute of Parallax in Altitude, and any Part of a Degree of Distance; and therefore, both of these Tables are contained in a much less Compass than this could be expressed Numerically in any manner whatever. At the same time, no proportional Parts ever come in question.

This Table is illustrated, in finding the last Correction for Refraction and Parallax, in the Examples farther on.

SECTION X.

Of TABLE V. in the Linear Tables.

In this Table, the Lines 1, 1; 2, 2; 3, 3; &c. do each of them contain 10 equal Parts. Therefore, if the Distance of any two Lines of the third Sort in Large Table I. be found among these Lines; any intermediate Distance between the Lines, is hereby easily found to a tenth Part of the whole.

This Method may be applied by help of a pair of compasses, to come to the greatest Accuracy by Table I. but it is not necessary in usual Practice. The Correction depending on Large Table I. is generally but small, except when one of the Altitudes is very small, and then (as hath been before noted, its Refraction cannot be depended on and a greater Error may arise therefrom. The peculiar Property of this Table, is that of giving Answer to a Multitude of Questions, instantly without proportional Parts, and all sufficiently exact for Use, although the Table is comprised in so small a Compass.

SECTION XI.

Of TABLE VI. in the Linear Tables.

This Table is a Supplement to Table II. and applied only when the lesser Altitude is from Eight to Four Degrees. In such Cases, the Distance of Centres is to be found in the Side of the Table to the nearest Ten Degrees, and against it is a Number of Seconds, which being subtracted from B, as it is taken from Table II. gives the Correct B, which is to be applied as directed in the Use of that Table.

SECTION

SECTION XII.

Of the PROPER LOGARITHMS, in the Linear Tables.

The Logarithms which are of most general Use are, first the Logarithms of Numbers, these are commonly called Common Logarithms; secondly, Log-fines, Log tangents and Log-secants.

When of four Terms in Direct Proportionality, three are given to find the fourth, and the first and third Terms do each consist of Minutes and Seconds, but the second Term is Unity; in order to take off the trouble of reducing the first and third Terms to Seconds, and other tedious Multiplication and Division, Proper Logarithms are applied which bring out the Answer by a single Subtraction.

Although these Proper Logarithms are commonly carried; to but four Places of Figures beside the Index, yet when Unity is the Middle Term, they are sufficient for this Purpose, because Unity is their Difference throughout almost all the last Quarter of the Table. In almost all the third Quarter the Difference is Two; throughout the second Quarter it is from Three to Five; and near the Middle of the first Quarter it is nine.

The same Logarithms may be made applicable, if Two, Three or Four, be the Middle Term, with this Alteration. If Two be the Middle Term, the Degrees Minutes and Seconds belonging to the respective Logarithms must be doubled; if Three be the Middle Term, the Logarithms must be trebled; if Four, they must be quadrupled, &c.

If they are trebled whilst the Logarithms remain the same, there will be either Uncertainty or Error of two Seconds of a Degree, in the last Quarter of the Table; and a Second of a Degree in a great Part of the third Quarter; and as often as these Errors are repeated in a Computation, so much greater is the Error thereby upon the whole.

The only apparent Remedy to these Defects, without working Proportional Parts, is the Bisection of the trebled Minutes and Seconds; for by this Method, in these uncertain Parts of the Table, whatever the Logarithm happens to be, its correspondent Number is taken out to the nearest Half Second by Inspection.

SECTION XIII.

A Description of the TABLE of PROPER LOGARITHMS.

At the Top of the Table are the Degrees and Minutes, marked in a successive Order to each Minute, and in the Side are the Seconds in

14 *Of the* PROPER LOGARITHMS.

in two Columns, to every Three Seconds, the innermost Column of Seconds belonging to the Logarithms, and the outermost belonging to the Medium of the two Logarithms one above and the other below the Line in which they stand. The left hand leading Figure or Figures of the Logarithms, repeat or are supposedly prefixed to those right hand Figures which are under them.

At the Bottom of the Table is a Row of Figures, shewing the mean Difference of the Logarithms in the Columns over which they stand; and underneath that is a Row of Degrees and Minutes, beginning with 0, and increasing by 15 Minutes of a Degree, to the End of the Table. At the outermost Column of Seconds, are small Marks a little above and below the Lines on which the Figures stand.

SECTION XIV.

How to take out the PROPER LOGARITHMS; and their Degrees, Minutes and Seconds.

1st. When the Degrees and Minutes are found at the Top of the Table, and the Seconds can be exactly had in the innermost Column at the Side, the Logarithm is at the Angle of Meeting in the Table.

2d. When the Seconds are found in the outside Column of the Table, the Medium of the right hand Figures of the Logarithm, with its prefixed left hand Figures, is the Logarithm required. In this Case, it appears by Inspection, that throughout almost all the latter half of the Table, the Differences of the Logarithms will not trisect; and that therefore they are not continued to Places enough for shewing the Logarithm to the nearest Second by such a Trisection.

3d. Since the inner and outer Columns of Seconds, do exhaust all Numbers in a successive order to the nearest Half Second, no Error whatever can happen by the above Method of using the second Half Part, nor an Error greater than Half a Second, by using the first Half Part of the Table. But, if greater Accuracy be wanted in the first Half of the Table, the Medium of the Logarithms compared with a given Logarithm, will shew whether the half Second is to be added to or subtracted from that in the outermost Column, to give the Truth required.

SECTION XV.

OF TABLE XII. in the Linear Tables.

This Table begins at 0, and goes on to either Three Hours or Three Degrees and shewing by Inspection both the Seconds of Time and

Of the LINEAR TABLES. 35

and the Seconds of a Degree; to either of which, add any given Number of Seconds, and the Total shews the Seconds in a given Number of either Hours, Minutes and Seconds, or of Degrees, Minutes and Seconds.

The Reverse of this turns Seconds into Time, or Degrees.

EXAMPLE I.

$$\begin{array}{rcl} \text{H} & & \text{M} \\ 2 & 27' & 53'' = 8873. \\ \text{for } 2 & 27 & 0 = 8820. \\ & & 53. \end{array}$$

EXAMPLE II.

$$\begin{array}{rcl} \text{H} & & \text{M} \\ 5679 & = & 1^{\text{h}} 34' 39'' \\ \text{for } 5649 & = & 1^{\text{h}} 34' 0. \\ & & 39. \end{array}$$

SECTION XVI.

Of TABLE XIII. in the Linear Tables.

This Table is of the same kind as that described in Section IV; as far as Sixty Minutes, which may likewise express Sixty Degrees. For Degrees above Sixty, this Table goes on by Tens to 360 Degrees or 24 Hours of Time.

SECTION XVII.

Of finding the True Distance of Centres of either Sun and Moon or Moon and Sun; having the Observed Distance of their Limbs.

In this work are two Formulas for computing not only the true Distance of Centres, but the whole Calculation for Longitude from Greenwich.

The first of these Formulas, finds the Effect of Refraction, which (in almost all practical Cases) is small, although the cases are numerous; and then the Effect of Parallax.

The second Formula works the joint Effect of Refraction and Parallax together.

The Longitude Instructions, shew the Order of these Operations, until Number E is found, in both Methods; then F is found, by the Directions in the Description and Use of Table IV.

When a Table consisting wholly of Numbers, increaseth descending perpendicularly but decreaseth horizontally, from one Degree to another, and Proportional Parts are to be worked for intermediate Minutes, this becomes a troublesome task to good Computers, and to indifferent ones it is sometimes insuperable. This was the case in Lyons's large Table I. and what put me under the necessity of substituting some easy Expedient affected with but small Error, which was that of the nearest whole Degree to those of the Observation.

By this Method the Difficulty was overcome, and the Error in usual

16 Of the TRUE DISTANCE of CENTRES.

usual Cases, seldom exceeded a few Seconds of a Degree; but this is wholly removed by the Construction and Use of the Linear Table I.

In the Use of this Table it is not necessary that the Computor should take out the third Figure in Thousandths Place to an Unit. Amongst the twenty two Examples following (which are almost all formed by such Data as would shew a Defect in this Table I. if there were any Defect in it) there is not one, but in it any Computor (however slow of apprehension) can take out the Number instantly without erring Five, and it might be said without erring Two in the greatest part of them. If that Error amounted to Ten (which can never happen under the least Judgment and Attention) the Errors thereby would be no more in Longitude at the Equinoctial, than the following; in the Channel the Miles would be but two thirds of those at the Equinoctial.

A View of the Errors at the Equinoctial, that would arise by increasing or diminishing the N^o taken out of Linear Table I. by an Error of Ten Units.

	Error Miles		Error Miles
Example I.	$4'' = 2$	Example XII.	$6'' = 3$
II.	$9 = 4\frac{1}{2}$	XIII.	$5 = 2\frac{1}{2}$
III.	— Absurdity.	XIV.	$3 = 1\frac{1}{2}$
IV.	— Absurdity.	XV.	$6 = 3$
V.	$2 = 1$	XVI.	$3 = 1\frac{1}{2}$
VI.	$2 = 1$	XVII.	— not used.
VII.	— not used.	XVIII.	$3 = 1\frac{1}{2}$
VIII.	$3 = 1\frac{1}{2}$	XIX.	— not used.
IX.	$3 = 1\frac{1}{2}$	XX.	— not used.
X.	— not used.	XXI.	$7 = 3\frac{1}{2}$
XI.	$4 = 2$	XXII.	$4 = 2$

The greatest Error that an indifferent Computor may happen to make in applying this Table, is when one Altitude is very small and the other very great; in such a Case, it appears from the Construction, that there cannot be an Error of Five in the third right hand Place, and this at the Equinoctial would produce an Error not exceeding Two Miles; in all other Cases the Error hereby would be less, and frequently vanish. But even in this particular Case, the Error through unknown Refraction near the Horizon, and an incorrect observed Distance of the Limbs, will be many times greater, and thereby render such as this of a very trifling Effect.

From such considerations as these, it will be easy to assign the Limits for greater and lesser Altitude, within which the Uncertainty of Refraction may not render the Longitude but little more affected with Error than what arises from the Imperfections of the Observations and Predictions in the Tables.

EXAMPLE

Of the TRUE DISTANCE of CENTRES 17

EXAMPLE I.

Distance observed $51^{\circ} 28' 35''$
 Star's Altitude $24^{\circ} 48' 5''$
 Moon's Altitude $12^{\circ} 30' 5''$
 Moon's Hor. Par. $0^{\circ} 56' 15''$
 Required the true Dist. of Centers?

1st. By Linear Tables.

N^o in Table I. - 2.136
 Co. ar. of Distance 0.107
 $175''$ Com. Log. Sum 2.243
 87 in Table II. $0^{\circ} 1' 28''$
 88 Correction $0^{\circ} 1' 28''$
 Dist. observed $51^{\circ} 28' 35''$
 $D = 51^{\circ} 30' 9''$
 1st Arc $= 0^{\circ} 30' 7''$
 2d Arc $= 0^{\circ} 9' 38''$
 $C = 0^{\circ} 20' 29''$
 $D = 51^{\circ} 30' 3''$
 $E = 51^{\circ} 9' 34''$
 $F = 0^{\circ} 0' 20''$
 $P = 51^{\circ} 9' 54''$

EXAMPLE II.

Distance observed $90^{\circ} 21' 13''$
 Star's Altitude $84^{\circ} 7' 6''$
 Moon's Altitude $5^{\circ} 17' 8''$
 Moon's Hor. Par. $1^{\circ} 1' 48''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. - 2.758
 Co. ar. of Distance 0.000
 $573''$ Com. Log. Sum 2.758
 0 in Table II: $0^{\circ} 1' 13''$
 573 Correction $0^{\circ} 9' 33''$
 Dist. observed $90^{\circ} 21' 13''$
 $D = 90^{\circ} 30' 46''$
 1st Arc $= 1^{\circ} 1' 29''$
 2d Arc $= 0^{\circ} 0' 3''$
 $C = 1^{\circ} 1' 32''$
 $D = 90^{\circ} 30' 46''$
 $E = 89^{\circ} 29' 14''$
 $F = 0^{\circ} 0' 1''$
 $P = 89^{\circ} 29' 13''$

2d. By Sun & Moon's Angles.

$M = 68^{\circ} 8'$
 $S = 93^{\circ} 38'$
 $A = 1133''$
 $B = 10$
 $C = 0^{\circ} 19' 3''$
 $D = 51^{\circ} 28' 35''$
 $E = 51^{\circ} 9' 32''$
 $F = 0^{\circ} 0' 20''$
 $P = 51^{\circ} 9' 52''$

2d. By Sun & Moon's Angles.

$M = 3^{\circ} 0'$
 $S = 17^{\circ} 20'$
 $A = 3119''$
 $B = 5$
 $C = 0^{\circ} 51' 54''$
 $D = 90^{\circ} 21' 13''$
 $E = 89^{\circ} 29' 19''$
 $F = 0^{\circ} 0' 1''$
 $P = 89^{\circ} 29' 20''$

3d. By different Methods.

1. By the Linear Tables $51^{\circ} 9' 54''$
 2. By Sun and Moon's Angles $51^{\circ} 9' 52''$
 3. By Lyons's whole Degrees $51^{\circ} 9' 51''$
 4. By Mr. Lyons himself $51^{\circ} 9' 52''$
 5. By Ditto altered - $51^{\circ} 9' 51''$
 6. By Mr. Dunthorne himself $51^{\circ} 9' 54''$
 7. By Ditto altered - $51^{\circ} 9' 51''$

3d. By different Methods.

1. By the Linear Tables $89^{\circ} 29' 13''$
 2. By Sun and Moon's Angles $89^{\circ} 29' 20''$
 3. By Lyons's whole Degrees $89^{\circ} 29' 17''$
 4. By Lyons altered - $89^{\circ} 29' 10''$
 5. By Dunthorne altered $89^{\circ} 29' 20''$
 6. By Ditto again altered $89^{\circ} 29' 15''$

D

EXAMPLE

18. Of the TRUE DISTANCE of CENTRES.

EXAMPLE III.

“Distance observed 89° 58' 6”
 Star's Altitude 5 6 5
 Moon's Altitude 88 46 5
 Moon's Hor. Par. 1 1 18
 Required the true Dist. of Centres?

1st. By Linear Tables.

Nº in Table I. 2.773
 Co. ar. of Dist. observed 0.000
 593" Com. Log. Sum 2.773
 0 in Table II. 0 1 11
 593 Correction 0 9 53
 Dist. observed 89 58 6
 D = 90 7 59
 1st Arc = 0 5 16
 2d Arc = 0 0 8
 C = 0 5 8
 D = 90 7 59
 E = 90 2 51
 F = 0 0 0
 P = 90 2 51

2d. By different Methods.

1. By the Linear Tables	90 2 51
2. By Sun & Moon's Angles, an Absurdity.	
3. By Lyons's whole Degrees	90 2 43
4. By Lyons altered	90 2 36
5. By Dunthorne altered	90 2 26
6. By Ditto again altered	90 2 32

EXAMPLE IV.

“Distance observed 103° 29' 27”
 Sun's Altitude 19 3 35
 Moon's Altitude 71 6 0
 Moon's Hor. Par. 0 58 34
 Required the true Dist. of Centres?

1st. By Linear Tables.

Nº in Table I. 2.265
 Co. ar. of Dist. observed 0.012
 189" Com. Log. Sum 2.277
 26 in Table II. 0 1 11
 215 Correction 0 3 35
 Dist. observed 103 29 27
 D = 103 29 27
 1st Arc = 0 19 38
 2d Arc = 0 13 21
 C = 0 32 59
 D = 103 33 2
 E = 103 0 3
 F = 0 0 0
 P = 103 0 3

2d. By different Methods.

1. By the Linear Tables	103 0 3
2. By Sun & Moon's Angles, an Absurdity.	
3. By Lyons's whole Degrees	103 0 4
4. By Lyons altered	102 59 54½
5. By Dunthorne altered	102 59 55
6. By Ditto again altered	102 59 56

The two foregoing Examples have nearly the same Data, as two of four published and solved in a certain Book of Tables; and these are here introduced, only to shew the Absurdity of such Questions.

When the Cotemporary Observations are made, the Observed Co-altitude of Sun or Star, the Observed Co-altitude of the Moon, and the Observed Distance of the Limbs, do always form a Spherical Triangle, in which any two of its Sides, are together greater than the third Side. But in both of these Questions, the two Co-altitudes together make less than the Distance; consequently, they are both of them absurd and unanswerable, and the Corrections for their Refraction and Parallax, belong to other Data.

EXAMPLE

A New and Easy FORMULA for the LONGITUDE by SUN and MOON. By S. Dunn

Central Dist. Hours at Greenw. " " " " " "

☉ & ☿ Limits observed.
☉ & ☿ true Semidiameter.
☿ true Semidiameter.
Parts for ☿'s Altitude.

Observed dist. of Centres. = L

Least Alt. Centre clear.
Greater Alt. Centre clear.
Parts by Top & Side Tab. 1
Dist. Centres (Co. ar.) 2.

A = Common Log ar.^m
B = Parts in Tab. II. add if the Dist. is above 90°.

add L =
D =

Hor. 1st Par.
☿'s Altitude.
Number D.
Proport. Log.^m
Co. Secant.
Sine.

1st Arc
Proport. Log.^m

Hor. 2^d Par.
☿'s Altitude.
Number D.
Proport. Log.^m
Co. Secant.
Tangent.

2^d Arc
Proport. Log.^m

C = Add the Arcs if D. is above 90°
D = Add C to D if ☿'s Arc is least & D. (is under 90°)

E =
F = Least Corr.ⁿ add if D. is under 90°

P = True Dist. of Centres.

Hours Hours
D.° Hours P

Diff. 1st Prop. Log.^m
Diff. 2^d Prop. Log.^m
Diff. 2^d Prop. Log.^m

Diff. of Log.^s in Prop. Log.^s
1st Hours add

Time at Greenw.

Co. lat.
a. Pole
Co. Alt.
2) Co. ar.
Co. ar.

1/2 Sum
Rem.
Sine
Sine

2) Co. ar.
Sine
Sine

Arc
16) 2 (Co. Sine
H " a Noon

Time at the Ship
Time at Greenw.

Ship's Longitude
or

The Co. ar. Sine, Tangent, &c. of Degrees when more than 90° is that of the Supp. to 180°. The Co. ar. is Co. Sec. less 10 in the Index. In this Formula, when Addition is not to be made subtraction must. For correct Time, at the Ship, see my New Epitome of Navigation.

A Formula for the Inverse having the Ephemeris & Common Tables of Logarithms. By S. Dunn Teacher of Mathematics London.

Rough Time • *H. Lat.*

Mr. T.!

Alt. 76.

© 1991 L!

Nearest Limbs:	0' " "
⊙ or * à Limbs obs. ^d	<i>Farthest Limb</i> "
⊙ Senidium ^r p. 3	* à Limb.....
⊙ Senidium ^r p. 7	⊙ Senid ^r
Parts for Δ Alt.	<i>Parts for Δ Alt.</i>
	<u>Sum sub.</u>
	0' " "
	Hours 0' " "
	=
	=
	Diff =
	Log.
	first Hour & Distance in Ephemeris
	second ditto

Sum is D =		Remainder is D =	
Altitude	Dip & Semid. chord.	or * Alt.	Dip & Semid. chord.
Coalt	co. ar.	or * Coalt	co. ar.
D	co. ar.	D	co. ar.
or * Coalt.		Coalt.	

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N.B. 1.st Rough central Distance shows the rough Hour at Greenwich & thereby the ☉ Declin.ⁿ is had Ephem. p. 2 (the ☉ Semid.^r is p. 3.) the ☉ Semid.^r & Hor. Par. p. 7. 2.^d O. ar. is Ascendant left in the Index. 3.^d O. ar. or Sine Dec. of more than 90. is of the Remain^r to 180°. 4.th Refraction to be taken from the Invert Tables. 5.th When you do not add subtract. 6.th O. alt. sub-tracted from ☉ Sum gives Remains^r. Polar Dist. is Dec.ⁿ & Lat.ⁿ alike, else added to 90°. 7.th If Time at Greenwich & at the Ship are both before or afternoon, their Difference is the Longitude, else it is what they are apart. 8.th Observe for Time at the Ship when ☉ is not near the Meridian. 9.th Reasons at large are in Astronomy p. 185 & Lon- gitude at Sea p. 90. 10.th Latitude is found at any Time of the Day by the common Instruments, as published by the Author, which see.

X

X

EXAMPLE V.

" Distance observed $110^{\circ} 22' 5''$
 Sun's Altitude $45^{\circ} 33' 36''$
 Moon's Altitude $19^{\circ} 43' 6''$
 Moon's Hor. Par. $0^{\circ} 57' 19''$
 Required the true Diff. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.163
 Co. ar. of Diff. observed 0.028
 $155''$ Com. Log. Sum 2.191
 41 in Table II. $0^{\circ} 1' 1''$
 196 Correction $0^{\circ} 3' 16''$
 Dist. observed $110^{\circ} 22' 5''$
 $D = 110^{\circ} 25' 21''$
 1^{st} Arc $= 0^{\circ} 57' 19''$
 2^{d} Arc $= 0^{\circ} 7' 11''$
 $C = 0^{\circ} 50' 50''$
 $D = 110^{\circ} 25' 21''$
 $E = 109^{\circ} 34' 31''$
 $F = 0^{\circ} 0' 1''$
 $P = 109^{\circ} 34' 30''$

2d. By Sun & Moon's Angles.

$M = 19^{\circ} 38'$
 $S = 27^{\circ} 56'$
 $A = 2902''$
 $B = 44''$
 $C = 0^{\circ} 47' 38''$
 $D = 110^{\circ} 22' 5''$
 $E = 109^{\circ} 34' 27''$
 $F = 0^{\circ} 0' 1''$
 $P = 109^{\circ} 34' 26''$

3d. By different Methods.

1. By the Linear Tables $109^{\circ} 34' 30''$
 2. By Sun and Moon's Angles $109^{\circ} 34' 26''$
 3. By Lyons's whole Degrees $109^{\circ} 34' 30''$
 4. By Lyons altered $109^{\circ} 34' 26''$

EXAMPLE VI.

" Distance observed $50^{\circ} 8' 41''$
 Star's Altitude $19^{\circ} 18' 5''$
 Moon's Altitude $55^{\circ} 56' 5''$
 Moon's Hor. Par. $1^{\circ} 0' 5''$
 Required the true Diff. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.215
 Co. ar. of Diff. observed 0.115
 $214''$ Com. Log. Sum 2.330
 91 in Table II. $0^{\circ} 1' 1''$
 123 Correction $0^{\circ} 2' 3''$
 Dist. observed $50^{\circ} 8' 41''$
 $D = 50^{\circ} 10' 44''$
 1^{st} Arc $= 0^{\circ} 25' 48''$
 2^{d} Arc $= 0^{\circ} 41' 29''$
 $C = 0^{\circ} 15' 41''$
 $D = 50^{\circ} 10' 44''$
 $E = 50^{\circ} 26' 25''$
 $F = 0^{\circ} 0' 5''$
 $P = 50^{\circ} 26' 30''$

2d. By Sun & Moon's Angles.

$M = 117^{\circ} 48'$
 $S = 31^{\circ} 42'$
 $A = 924''$
 $B = 137''$
 $C = 0^{\circ} 17' 41''$
 $D = 50^{\circ} 8' 41''$
 $E = 50^{\circ} 26' 22''$
 $F = 0^{\circ} 0' 5''$
 $P = 50^{\circ} 26' 27''$

3d. By different Methods.

1. By the Linear Tables $50^{\circ} 26' 30''$
 2. By Sun and Moon's Angles $50^{\circ} 26' 27''$
 3. By Lyons's whole Degrees $50^{\circ} 26' 29''$
 4. By Ditto altered $50^{\circ} 26' 29''$
 5. By Dunthorne altered $50^{\circ} 26' 28''$

D 2

EXAMPLE

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EXAMPLE VII.

"Distance observed $28^{\circ} 14' 39''$
 Star's Altitude $20^{\circ} 11' 4''$
 Moon's Altitude $18^{\circ} 56' 4''$
 Moon's Hor. Par. $0^{\circ} 55' 30''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table III. $0^{\circ} 0' 30''$
 Dist. observed $28^{\circ} 14' 39''$
 D = $28^{\circ} 15' 9''$
 1st Arc = $0^{\circ} 40' 22''$
 2d Arc = $0^{\circ} 33' 26''$
 C = $0^{\circ} 6' 56''$
 D = $28^{\circ} 15' 9''$
 E = $28^{\circ} 8' 13''$
 F = $0^{\circ} 0' 44''$
 P = $28^{\circ} 8' 57''$

2d. By Sun & Moon's Angles,

M = $82^{\circ} 24'$
 S = $87^{\circ} 22''$
 A = 395
 B = 8
 C = $0^{\circ} 6' 27''$
 D = $28^{\circ} 14' 39''$
 E = $28^{\circ} 8' 12''$
 F = $0^{\circ} 0' 44''$
 P = $28^{\circ} 8' 56''$

3d. By different Methods.

1. By the Linear Tables $28^{\circ} 8' 57''$
 2. By Sun and Moon's Angles $28^{\circ} 8' 56''$
 3. By Lyons's whole Degrees $28^{\circ} 8' 56''$
 4. By Ditto altered $28^{\circ} 8' 57''$

EXAMPLE VIII.

"Distance observed $59^{\circ} 25' 34''$
 Sun's Altitude $59^{\circ} 12' 5''$
 Moon's Altitude $27^{\circ} 2' 5''$
 Moon's Hor. Par. $0^{\circ} 59' 58''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.136
 Co. ar. of Dist. observed 0.065
 159'' Com. Log. Sum 2.201
 65 in Table II. $0^{\circ} 1' 34''$
 94 Correction $0^{\circ} 1' 34''$
 Dist. observed $59^{\circ} 25' 34''$
 D = $59^{\circ} 27' 8''$
 1st Arc = $0^{\circ} 59' 48''$
 2d Arc = $0^{\circ} 16' 4''$
 C = $0^{\circ} 43' 44''$
 D = $59^{\circ} 27' 8''$
 E = $58^{\circ} 43' 24''$
 F = $0^{\circ} 0' 5''$
 P = $58^{\circ} 43' 29''$

2d. By Sun & Moon's Angles.

M = $35^{\circ} 4'$
 S = $87^{\circ} 42''$
 A = 2533
 B = 1
 C = $0^{\circ} 42' 12''$
 D = $59^{\circ} 25' 34''$
 E = $58^{\circ} 43' 22''$
 F = $0^{\circ} 0' 5''$
 P = $58^{\circ} 43' 27''$

3d. By different Methods.

1. By the Linear Tables $58^{\circ} 43' 29''$
 2. By Sun and Moon's Angles $58^{\circ} 43' 27''$
 3. By Lyons's whole Degrees $58^{\circ} 43' 26''$
 4. By Ditto altered $58^{\circ} 43' 29''$

EXAMPLE

Of the TRUE DISTANCE of CENTRES. 21

EXAMPLE IX.

“Distance observed $43^{\circ} 35' 42''$
 Star's Altitude $11^{\circ} 18' 6''$
 Moon's Altitude $9^{\circ} 37' 6''$
 Moon's Hor. Par. $0^{\circ} 54' 42''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.052
 Co. ar. of Dist. observed 0.161
 163ⁿ Com. Log. Sum 2.213
 118 in Table II.
 45 Correction $0^{\circ} 0' 45''$
 Dist. observed $43^{\circ} 35' 42''$
 $D = 43^{\circ} 36' 27''$
 1st Arc $= 0^{\circ} 15' 24''$
 2d Arc $= 0^{\circ} 9' 32''$
 $C = 0^{\circ} 5' 52''$
 $D = 43^{\circ} 36' 27''$
 $E = 43^{\circ} 30' 35''$
 $F = 0^{\circ} 0' 26''$
 $P = 43^{\circ} 31' 1''$

2d. By Sun & Moon's Angles.

$M = 83^{\circ} 43'$
 $S = 87^{\circ} 50'$
 $A = 319''$
 $B = 11''$
 $C = 0^{\circ} 5' 8''$
 $D = 43^{\circ} 35' 42''$
 $E = 43^{\circ} 30' 34''$
 $F = 0^{\circ} 0' 26''$
 $P = 43^{\circ} 31' 0''$

3d. By different Methods.

1. By the Linear Tables $43^{\circ} 31' 1''$
 2. By Sun and Moon's Angles $42^{\circ} 31' 0''$
 3. By Lyons's whole Degrees $43^{\circ} 31' 1''$
 4. By Astronomer Royal $43^{\circ} 31' 2''$

EXAMPLE X.

“Distance observed $29^{\circ} 24' 46''$
 Star's Altitude $49^{\circ} 57' 4''$
 Moon's Altitude $64^{\circ} 19' 4''$
 Moon's Hor. Par. $0^{\circ} 57' 8''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table III. $0^{\circ} 0' 31''$
 Dist. observed $29^{\circ} 24' 46''$
 $D = 29^{\circ} 25' 17''$
 1st Arc $= 1^{\circ} 44' 50''$
 2d Arc $= 1^{\circ} 17' 34''$
 $C = 0^{\circ} 27' 16''$
 $D = 29^{\circ} 25' 17''$
 $E = 28^{\circ} 58' 1''$
 $F = 0^{\circ} 0' 7''$
 $P = 28^{\circ} 58' 8''$

2d. By Sun & Moon's Angles.

$M = 42^{\circ} 4'$
 $S = 95^{\circ} 19'$
 $A = 1602''$
 $B = 2''$
 $C = 0^{\circ} 26' 44''$
 $D = 29^{\circ} 24' 46''$
 $E = 28^{\circ} 58' 2''$
 $F = 0^{\circ} 0' 7''$
 $P = 28^{\circ} 58' 9''$

3d. By different Methods.

1. By the Linear Tables $28^{\circ} 58' 8''$
 2. By Sun and Moon's Angles $28^{\circ} 58' 9''$
 3. By Lyons's whole Degrees $28^{\circ} 58' 9''$
 4. By Witchell's Method $28^{\circ} 58' 21''$

EXAMPLE

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EXAMPLE XI.

"Distance observed $62^{\circ} 23' 59''$
 Star's Altitude $18^{\circ} 42' 6''$
 Moon's Altitude $47^{\circ} 42' 6''$
 Moon's Hor. Par. $0^{\circ} 57' 6''$

Required the true Dist. of Centres.

1st. By Linear Tables.

N^o in Table I. 2.188
 Co. ar. of Dist. observed 0.052
 174" Com. Log. Sum 2.240
 58 in Table II. $0^{\circ} 1' 56''$
 116 Correction $0^{\circ} 1' 56''$
 Dist. observed $62^{\circ} 23' 59''$
 D = $62^{\circ} 25' 55''$
 1st Arc = $0^{\circ} 20' 36''$
 2d Arc = $0^{\circ} 22' 3''$
 C = $0^{\circ} 1' 27''$
 D = $62^{\circ} 25' 55''$
 E = $62^{\circ} 27' 22''$
 F = $0^{\circ} 0' 5''$
 P = $62^{\circ} 27' 27''$

2d. By Sun & Moon's Angles.

M = $92^{\circ} 8'$
 S = $45^{\circ} 15'$
 A = $84''$
 B = $116''$
 C = $0^{\circ} 3' 20''$
 D = $62^{\circ} 23' 59''$
 E = $62^{\circ} 27' 19''$
 F = $0^{\circ} 0' 5''$
 P = $62^{\circ} 27' 24''$

3d. By different Methods.

1. By the Linear Tables $62^{\circ} 27' 27''$
 2. By Sun and Moon's Angles $62^{\circ} 27' 24''$
 3. By Lyons's whole Degree $62^{\circ} 27' 26''$
 4. By Witchell's Method $62^{\circ} 27' 27''$

EXAMPLE XII.

"Distance observed $85^{\circ} 0' 0''$
 Star's Altitude $5^{\circ} 0' 5''$
 Moon's Altitude $30^{\circ} 0' 5''$
 Moon's Hor. Par. $1^{\circ} 0' 0''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.480
 Co. ar. of Dist. observed 0.002
 303" Com. Log. Sum 2.482
 9 in Table II. $0^{\circ} 4' 54''$
 294 Correction $0^{\circ} 4' 54''$
 Dist. observed $85^{\circ} 0' 0''$
 D = $85^{\circ} 4' 54''$
 1st Arc = $0^{\circ} 5' 4''$
 2d Arc = $0^{\circ} 2' 34''$
 C = $0^{\circ} 2' 30''$
 D = $85^{\circ} 4' 54''$
 E = $85^{\circ} 2' 24''$
 F = $0^{\circ} 0' 2''$
 P = $85^{\circ} 2' 26''$

2d. By Sun & Moon's Angles.

M = $87^{\circ} 6'$
 S = $60^{\circ} 12'$
 A = $153''$
 B = $295''$
 C = $0^{\circ} 2' 22''$
 D = $85^{\circ} 0' 0''$
 E = $85^{\circ} 2' 22''$
 F = $0^{\circ} 0' 2''$
 P = $85^{\circ} 2' 24''$

3d. By different Methods.

1. By the Linear Tables $85^{\circ} 2' 26''$
 2. By Sun and Moon's Angles $85^{\circ} 2' 24''$
 3. By Lyons's whole Degree $85^{\circ} 2' 31''$
 4. By Witchell's Method $85^{\circ} 2' 27''$

EXAMPLE

EXAMPLE XIII.

" Distance observed $38^{\circ} 22' 17''$
 Star's Altitude $12^{\circ} 27' 5''$
 Moon's Altitude $20^{\circ} 9' 4''$
 Moon's Hor. Par. $0^{\circ} 57' 24''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.095
 Co. ar. of Dist. observed 0.207
 201" Com. Log. Sum 2.302
 140 in Table II. $0^{\circ} 1' 1''$
 61 Correction $0^{\circ} 1' 1''$
 Dist. observed $38^{\circ} 22' 17''$
 $D = 38^{\circ} 23' 18''$
 1st Arc $= 0^{\circ} 19' 49''$
 2d Arc $= 0^{\circ} 24' 54''$
 $C = 0^{\circ} 5' 5''$
 $D = 38^{\circ} 23' 18''$
 $E = 38^{\circ} 28' 23''$
 $F = 0^{\circ} 0' 31''$
 $P = 38^{\circ} 28' 54''$

2d. By Sun & Moon's Angles.

$M = 95^{\circ} 22'$
 $S = 73^{\circ} 12''$
 $A = 288$
 $B = 73$
 $C = 0^{\circ} 6' 1''$
 $D = 38^{\circ} 22' 17''$
 $E = 38^{\circ} 28' 18''$
 $F = 0^{\circ} 0' 31''$
 $P = 38^{\circ} 28' 49''$

3d. By different Methods.

1. By the Linear Tables $38^{\circ} 28' 54''$
 2. By Sun and Moon's Angles $38^{\circ} 28' 49''$
 3. By Lyons's whole Degrees $38^{\circ} 28' 59''$
 4. By Cambridge Tables $38^{\circ} 28' 56''$

EXAMPLE XIV.

" Distance observed $45^{\circ} 40' 14''$
 Star's Altitude $15^{\circ} 54' 4''$
 Moon's Altitude $21^{\circ} 26' 4''$
 Moon's Hor. Par. $0^{\circ} 56' 30''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.074
 Co. ar. of Dist. observed 0.146
 166' Com. Log. Sum 2.220
 109 in Table II. $0^{\circ} 1' 7''$
 57 Correction $0^{\circ} 0' 57''$
 Dist. observed $45^{\circ} 40' 14''$
 $D = 45^{\circ} 41' 11''$
 1st Arc $= 0^{\circ} 21' 35''$
 2d Arc $= 0^{\circ} 20' 27''$
 $C = 0^{\circ} 1' 28''$
 $D = 45^{\circ} 41' 11''$
 $E = 45^{\circ} 39' 43''$
 $F = 0^{\circ} 0' 23''$
 $P = 45^{\circ} 40' 6''$

2d. By Sun & Moon's Angles.

$M = 88^{\circ} 25'$
 $S = 75^{\circ} 22''$
 $A = 83$
 $B = 50$
 $C = 0^{\circ} 0' 33''$
 $D = 45^{\circ} 40' 14''$
 $E = 45^{\circ} 39' 41''$
 $F = 0^{\circ} 0' 23''$
 $P = 45^{\circ} 40' 4''$

3d. By different Methods.

1. By the Linear Tables $45^{\circ} 40' 6''$
 2. By Sun and Moon's Angles $45^{\circ} 40' 4''$
 3. By Lyons's whole Degrees $45^{\circ} 40' 1''$
 4. By Cambridge Tables $45^{\circ} 40' 7''$

EXAMPLE

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EXAMPLE XV.

"Distance observed $65^{\circ} 27' 30''$
 Star's Altitude $78^{\circ} 18' 6''$
 Moon's Altitude $15^{\circ} 21' 6''$
 Moon's Hor. Par. $1^{\circ} 0' 25''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.349
 Co. ar. of Dist. observed 0.041
 246" Com. Log. Sum 2.390
 50 in Table II. $0^{\circ} 3' 16''$
 196 Correction $0^{\circ} 3' 16''$
 Dist. observed $65^{\circ} 27' 30''$
 $D = 65^{\circ} 30' 46''$
 1st Arc = $1^{\circ} 5' 1''$
 2d Arc = $0^{\circ} 7' 11''$
 $C = 0^{\circ} 57' 50''$
 $D = 65^{\circ} 30' 46''$
 $E = 64^{\circ} 32' 56''$
 $F = 0^{\circ} 0' 1''$
 $P = 64^{\circ} 32' 57''$

2d. By Sun & Moon's Angles.

$M = 7^{\circ} 46'$
 $S = 140^{\circ} 24'$
 $A = 3259$
 $B = 9$
 $C = 0^{\circ} 54' 28''$
 $D = 65^{\circ} 27' 30''$
 $E = 64^{\circ} 33' 2''$
 $F = 0^{\circ} 0' 1''$
 $P = 64^{\circ} 33' 3''$

3d. By different Methods.

1. By the Linear Tables $64^{\circ} 32' 57''$
 2. By Sun and Moon's Angles $64^{\circ} 33' 3''$
 3. By Lyons's whole Degree $64^{\circ} 32' 59''$
 4. By Cambridge Tables $64^{\circ} 32' 59''$

EXAMPLE XVI.

"Distance observed $49^{\circ} 17' 21''$
 Star's Altitude $27^{\circ} 15' 5''$
 Moon's Altitude $43^{\circ} 20' 5''$
 Moon's Hor. Par. $0^{\circ} 58' 50''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.090
 Co. ar. of Dist. observed 0.120
 162" Com. Log. Sum 2.210
 95 in Table II. $0^{\circ} 1' 7''$
 67 Correction $0^{\circ} 1' 7''$
 Dist. observed $49^{\circ} 17' 21''$
 $D = 49^{\circ} 18' 28''$
 1st Arc = $0^{\circ} 35' 30''$
 2d Arc = $0^{\circ} 34' 44''$
 $C = 0^{\circ} 0' 46''$
 $D = 49^{\circ} 18' 28''$
 $E = 49^{\circ} 17' 42''$
 $F = 0^{\circ} 0' 13''$
 $P = 49^{\circ} 17' 55''$

2d. By Sun & Moon's Angles.

$M = 88^{\circ} 57'$
 $S = 54^{\circ} 53'$
 $A = 46$
 $B = 64$
 $C = 0^{\circ} 0' 18''$
 $D = 49^{\circ} 17' 21''$
 $E = 49^{\circ} 17' 39''$
 $F = 0^{\circ} 0' 13''$
 $P = 49^{\circ} 17' 52''$

3d. By different Methods.

1. By the Linear Tables $49^{\circ} 17' 55''$
 2. By Sun and Moon's Angles $49^{\circ} 17' 52''$
 3. By Lyons's whole Degrees $49^{\circ} 17' 54''$
 4. By Cambridge Tables $49^{\circ} 17' 54''$

EXAMPLE

Of the TRUE DISTANCE of CENTRES. 25

EXAMPLE XVII.

Distance observed $35^{\circ} 29' 45''$
 Star's Altitude $17^{\circ} 40' 5''$
 Moon's Altitude $20^{\circ} 34' 5''$
 Moon's Hor. Par. $0^{\circ} 56' 24''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table III. $0^{\circ} 0' 37''$
 Dist. observed $35^{\circ} 29' 45''$
 D = $35^{\circ} 30' 22''$
 1st Arc = $0^{\circ} 29' 24''$
 2d Arc = $0^{\circ} 27' 44''$
 C = $0^{\circ} 1' 40''$
 D = $35^{\circ} 30' 22''$
 E = $35^{\circ} 28' 42''$
 F = $0^{\circ} 0' 33''$
 P = $35^{\circ} 29' 15''$

2d. By Sun & Moon's Angles.

M = $88^{\circ} 9'$
 S = $79^{\circ} 8''$
 A = $97'$
 B = $33''$
 C = $0^{\circ} 1' 4''$
 D = $35^{\circ} 29' 45''$
 E = $35^{\circ} 28' 41''$
 F = $0^{\circ} 0' 33''$
 P = $35^{\circ} 29' 14''$

3d. By different Methods.

1. By the Linear Tables $35^{\circ} 29' 15''$
 2. By Sun and Moon's Angles $35^{\circ} 29' 14''$
 3. By Lyons's whole Degrees $35^{\circ} 29' 14''$
 4. By Cambridge Tables $35^{\circ} 29' 20''$

EXAMPLE XVIII.

Distance observed $102^{\circ} 30' 0''$
 Star's Altitude $15^{\circ} 23' 5''$
 Moon's Altitude $27^{\circ} 30' 5''$
 Moon's Hor. Par. $0^{\circ} 57' 3''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.112
 Co. ar. of Dist. observed 0.010
 133'' Com. Log. Sum 2.122
 24 in Table H. $0^{\circ} 1' 11''$
 157 Correction $0^{\circ} 2' 37''$
 Dist. observed $102^{\circ} 30' 0''$
 D = $102^{\circ} 32' 37''$
 1st Arc = $0^{\circ} 15' 29''$
 2d Arc = $0^{\circ} 5' 51''$
 C = $0^{\circ} 21' 20''$
 D = $102^{\circ} 32' 37''$
 E = $102^{\circ} 11' 17''$
 F = $0^{\circ} 0' 5''$
 P = $102^{\circ} 11' 12''$

2d. By Sun & Moon's Angles.

M = $65^{\circ} 0'$
 S = $56^{\circ} 30''$
 A = $1237'$
 B = $113''$
 C = $0^{\circ} 18' 44''$
 D = $102^{\circ} 30' 0''$
 E = $102^{\circ} 11' 16''$
 F = $0^{\circ} 0' 5''$
 P = $102^{\circ} 11' 11''$

3d. By different Methods.

1. By the Linear Tables $102^{\circ} 11' 12''$
 2. By Sun and Moon's Angles $102^{\circ} 11' 11''$
 3. By Lyons's whole Degrees $102^{\circ} 11' 15''$
 4. By Ditto himself $102^{\circ} 11' 11''$
 5. By 12 Case Method $102^{\circ} 10' 54''$

E

EXAMPLE

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EXAMPLE XIX.

Distance observed $33^{\circ} 15' 0''$
 Star's Altitude $48^{\circ} 20' 5''$
 Moon's Altitude $64^{\circ} 30' 5''$
 Moon's Hor. Par. $0^{\circ} 55' 29''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table III. $0^{\circ} 0' 35''$
 Dist. observed $33^{\circ} 15' 0''$
 D = $33^{\circ} 15' 35''$
 1st Arc = $1^{\circ} 15' 33''$
 2d Arc = $1^{\circ} 16' 21''$
 C = $0^{\circ} 0' 48''$
 D = $33^{\circ} 15' 35''$
 E = $33^{\circ} 16' 23''$
 F = $0^{\circ} 0' 6''$
 P = $33^{\circ} 16' 29''$

2d. By Sun & Moon's Angles.

M = $91^{\circ} 58'$
 S = $40^{\circ} 25'$
 A = $48''$
 B = $38''$
 C = $0^{\circ} 1' 26''$
 D = $33^{\circ} 15' 0''$
 E = $33^{\circ} 16' 26''$
 F = $0^{\circ} 0' 6''$
 P = $33^{\circ} 16' 32''$

3d. By different Methods.

1. By the Linear Tables $33^{\circ} 16' 29''$
 2. By Sun and Moon's Angles $33^{\circ} 16' 32''$
 3. By Lyons's whole Degrees $33^{\circ} 16' 29''$
 4. By Ditto himself $33^{\circ} 16' 29''$

EXAMPLE XX.

Distance observed $56^{\circ} 17' 44''$
 Star's Altitude $53^{\circ} 13' 8''$
 Moon's Altitude $64^{\circ} 38' 4''$
 Moon's Hor. Par. $1^{\circ} 1' 9''$
 Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table III. $0^{\circ} 1' 1''$
 Dist. observed $56^{\circ} 17' 44''$
 D = $56^{\circ} 18' 45''$
 1st Arc = $0^{\circ} 58' 50''$
 2d Arc = $0^{\circ} 36' 49''$
 C = $0^{\circ} 22' 1''$
 D = $56^{\circ} 18' 45''$
 E = $55^{\circ} 56' 44''$
 F = $0^{\circ} 0' 0''$
 P = $55^{\circ} 56' 44''$

2d. By Sun & Moon's Angles.

M = $32^{\circ} 16'$
 S = $21^{\circ} 50'$
 A = $1406''$
 B = $40''$
 C = $0^{\circ} 21' 6''$
 D = $56^{\circ} 17' 44''$
 E = $55^{\circ} 56' 38''$
 F = $0^{\circ} 0' 0''$
 P = $55^{\circ} 56' 38''$

3d. By different Methods.

1. By the Linear Tables $55^{\circ} 56' 44''$
 2. By Sun and Moon's Angles $55^{\circ} 56' 38''$
 3. By Lyons's whole Degrees $55^{\circ} 56' 45''$
 4. By Ditto himself $55^{\circ} 56' 46''$
 5. By 12 Cafe Method $55^{\circ} 56' 50''$

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Of the TRUE DISTANCE of CENTRES 27

EXAMPLE XXI.

"Distance observed $113^{\circ} 19' 26''$
 Sun's Altitude $5^{\circ} 1' 5''$
 Moon's Altitude $29^{\circ} 38' 5''$
 Moon's Hor. Par. $0^{\circ} 56' 29''$

Required the true Dist. of Centres.

1st. By Linear Tables.

N^o in Table I. 2.478
 Co. ar. of Dist. observed 0.037
 328" Com. Log. Sum 2.515
 48 in Table II. 0
 376 Correction $0^{\circ} 6' 16''$
 Dist. observed $113^{\circ} 19' 26''$
 D = $113^{\circ} 25' 42''$
 1st Arc = $0^{\circ} 5' 13''$
 2d Arc = $0^{\circ} 12' 6''$
 C = $0^{\circ} 17' 19''$
 D = $113^{\circ} 25' 42''$
 E = $113^{\circ} 8' 23''$
 F = $0^{\circ} 0' 9''$
 P = $113^{\circ} 8' 14''$

2d. By Sun & Moon's Angles.

M = $69^{\circ} 13'$
 S = $54^{\circ} 39''$
 A = 1010
 B = 339
 C = $0^{\circ} 11' 11''$
 D = $113^{\circ} 19' 26''$
 E = $113^{\circ} 8' 15''$
 F = $0^{\circ} 0' 9''$
 P = $113^{\circ} 8' 6''$

3d. By different Methods.

1. By the Linear Tables $113^{\circ} 8' 14''$
 2. By Sun and Moon's Angles $113^{\circ} 8' 6''$
 3. By Lyons's whole Degrees $113^{\circ} 8' 19''$
 4. By Witchell's Method $113^{\circ} 8' 12''$

EXAMPLE XXII.

"Distance observed $101^{\circ} 46' 43''$
 Sun's Altitude $56^{\circ} 16' 0''$
 Moon's Altitude $17^{\circ} 47' 0''$
 Moon's Hor. Par. $0^{\circ} 56' 40''$

Required the true Dist. of Centres?

1st. By Linear Tables.

N^o in Table I. 2.240
 Co. ar. of Dist. observed 0.009
 177" Com. Log. Sum 2.249
 22 in Table II. 0
 199 Correction $0^{\circ} 3' 19''$
 Dist. observed $101^{\circ} 46' 43''$
 D = $101^{\circ} 46' 43''$
 1st Arc = $0^{\circ} 48' 9''$
 2d Arc = $0^{\circ} 3' 37''$
 C = $0^{\circ} 51' 46''$
 D = $101^{\circ} 50' 2''$
 E = $100^{\circ} 58' 16''$
 F = $0^{\circ} 0' 1''$
 P = $100^{\circ} 58' 15''$

2d. By Sun & Moon's Angles.

M = $16^{\circ} 22'$
 S = $35^{\circ} 6''$
 A = 2936
 B = 28
 C = $0^{\circ} 48' 28''$
 D = $101^{\circ} 46' 43''$
 E = $100^{\circ} 58' 15''$
 F = $0^{\circ} 0' 1''$
 P = $100^{\circ} 58' 14''$

3d. By different Methods.

1. By the Linear Tables $100^{\circ} 58' 15''$
 2. By Sun and Moon's Angles $100^{\circ} 58' 14''$
 3. By Lyons's whole Degree $100^{\circ} 58' 17''$
 4. By Witchell's Method $100^{\circ} 58' 0''$

SECTION

28 OF TIME at GREENWICH and at the SHIP.

SECTION XVIII.

Of the TIME at GREENWICH and at the SHIP.

The Time at Greenwich and at the Ship, may be expressed either in Hours, Minutes and Seconds, or in Degrees, Minutes and Seconds, allowing Fifteen Degrees to an Hour of Time; but it will be most easy and expeditious to use the latter of these two methods; nevertheless, either of them may be used, as it may be thought most adviseable.

The lowermost Line in the table of Proper Logarithms, increases by Fifteen Minutes to Forty-five Degrees. The uppermost Line increases to Three Degrees, which may also be called Three Hours of Time.

When the last Difference of Proper Logarithms is found; if Hours are to express the Time at Greenwich, the Degrees and Minutes at Top are Hours and Minutes, and the Seconds are in the side of the Table; to these add the first Hours, and the Time at Greenwich is had in Time.

If the Time at Greenwich, is to be expressed in Degrees, a Fourth part of the Seconds in the Side are Minutes to be added to the Degrees and Minutes in the lowermost line of the Table, and this added to the first Hours in Degrees, gives the Time at Greenwich in Degrees and Minutes.

By the same Method, the Time at the Ship, either past Noon or short of Noon, is found in Degrees and Minutes; and these compared with the Time at Greenwich, gives the Longitude.

This easy Method of avoiding the several Reductions into Time, was first pointed out in the *Theory and Practice of Longitude* and Formule therewith; and is unexceptionable, as the Time at the Ship is to be applied to that at Greenwich, in the same manner whilst it is in Degrees, as it would be if it was in Time.

When a Watch is set for shewing the Time at the Ship or rather at the Meridian where Observations have been made for its adjustment; the Reductions to Time are to be made in the usual manner.

The Expression for Longitude is and ever will be in Degrees and not Time, because the Charts are instituted on that Plan, and the whole System of Astronomical Calculations and Tables. It would therefore be, not only best for the Ease of the Longitude Computor, but most exact (if he must use a Watch for shewing Time at the Ship) to get one that shews Degrees and Minutes of the Equator, as such an one would be also more readily applied to the other Methods of finding Longitude at Sea, and other parts of Practical Astronomy; but in such case, the Equation Tables and all others must be regulated accordingly.

SECTION

EXAMPLE

Of TIME at GREENWICH and at the SHIP. 29

EXAMPLE I.

H	=	73	1	27
6	=	74	28	50
		1	27	23
Proper Log.	=	0.3139		
3	=	73	1	27
P	=	74	11	58
		1	10	31
Proper Log.	=	0.4070		
		36	19	= 0.0931
		45	0	
Time		81	19	Gr. P. M.
Co-lat.		55	43	= 0.0829
Pol. dist.		84	12	= 0.0022
Co-alt.		70	38	
		210	33	
		105	16	= 9.9844
		34	38	= 9.7546
				19.8241
		35	15	= 9.91205
Time		70	30	Ship P. M.
Longitude		10	49	W.

EXAMPLE II.

H	=	108	5	58
6	=	109	37	16
		1	31	18
Proper Log.	=	0.2948		
3	=	108	5	58
P	=	109	34	26
		1	28	28
Proper Log.	=	0.3085		
		43	36	= 0.0137
		45		
Time		88	36	Gr. P. M.
Co-lat.		56	23	= 0.0795
Pol. dist.		67	25	= 0.0346
Co-alt.		44	28	
		168	16	
		84	8	= 9.9977
		39	40	= 9.8050
				19.9168
		24	40	= 9.9584
Time		49	21	Ship P. M.
Longitude		39	59	W.

EXAMPLE III.

H	=	93	57	36
9	=	95	32	11
		1	34	35
Proper Log.	=	0.2795		
6	=	93	57	36
P	=	95	18	6
		1	20	30
Proper Log.	=	0.3495		
		38	18	= 0.0700
		90	0	
Time		128	18	Gr. P. M.
Co-lat.		69	30	= 0.0284
Pol. dist.		100	46	= 0.0077
Co-alt.		50	19	
		220	35	
		110	17	= 9.9722
		59	58	= 9.9374
				19.9457
		20	3	= 9.97285
Time		40	6	Ship P. M.
Longitude		88	12	W.

During ten years till 1777 it was thought absolutely necessary to have a good Watch for shewing Time at the Ship, but this was exploded by my Formula for that purpose, and more particularly the year following in the Theory and Practice of Longitude at Sea; because the Time at the Ship is easily determined from the Latitude and the Cotemporary Observations. Whereas, 1st. The Watch may not be set right. 2d. It may not go right. 3d. The Course may not be truly known. 4th. The Variation may not be known. 5th. The Distance may not be truly measured. When the Time so carried is great, and several of these Errors are of the same kind, the amount may be considerable, and therefore it behoves every person practicing this Method to avoid as much as possible, these Errors.

SECTION

30 Of the PLANETS and ZODIACAL STARS.

SECTION XIX.

Of the apparent Places, Diurnal Motions and Periodic Revolutions of the Sun, Moon, Primary Planets and Fixed Stars.

1. The Sun is always apparently in the Ecliptic Line, and therefore hath Right Ascension, Declination and Longitude, but no Latitude.

2. The Moon is always apparently near the Ecliptic, sometimes a few degrees north or south thereof, at other times in it; and therefore may have Right Ascension and Declination, Longitude and Latitude.

3. Mercury and Venus; Mars, Jupiter and Saturn, are always apparently near the Ecliptic, and therefore may have Right Ascension and Declination, Longitude and Latitude.

4. Some of the Fixed Stars are near and others remote from the Ecliptic; therefore, they may have Right Ascension and Declination, Longitude and Latitude.

Of the Diurnal Motions.

5. The Sun apparently moves round the Earth, in the Interval of Time called a Solar Day.

6. The Moon apparently moves round the Earth at a Medium, in an Interval which is 52 Minutes longer than a Solar Day.

7. The Primary Planets may apparently move round the Earth, either in a Solar Day or a little longer or shorter Interval, according to their Places in the Heavens.

8. The fixed Stars apparently move round the Earth in a shorter Interval of Time than the Sun, by almost a Degree of the Equator or 3.57" of Time.

Of the Periodic Revolutions:

9. The Sun apparently moves round the Ecliptic in the Interval of a Solar Year, or 365 Days 5 Hours 49 Minutes.

10. The Moon apparently moves round the Ecliptic, or rather near it, in 27 Days 7 hours 43 Minutes; but it is 29 Days and near 13 Hours, by the Time she comes to the same apparent Longitude with the Sun.

11. The Primary Planets are near the Sun, as follows; namely, Mercury in 58 Days; Venus in 292 Days; Mars in 780 Days; Jupiter in 398 Days; Saturn in 378 Days. Therefore, in these Intervals, they come nearly to their like apparent Distances from the Sun.

12. The

Of the ZODIACAL STARS. 31

12. The Fixed Stars apparently move round the Poles of the Ecliptic in an Interval of 25920 Years.

SECTION XX.

Of the Places of the Zodiacal Stars.

1. The Zodiac is a Space of near 17 Degrees in Breadth, extending round the Heavens, and divided in the Middle by the Ecliptic Line.

2. The Fixed Stars within the Bounds of the Zodiac are called the Zodiacal Stars. Those of the first Magnitude either within this Limit, or not far north or south from it, are used in finding the Longitude at Sea in the Night, in the Lunar Method.

3. The Zodiacal Stars of greater Appearance within the Zodiac, are

1st. ALDEBARAN; a Red Star having many small Stars round it, and the Seven Stars to its northwest.

2d. POLLUX about 45° eastward from Aldebaran, having Castor a Star of the same Magnitude, north westwardly from it.

3d. REGULUS; a Red Star, about 37° southeastward from Pollux, known by being southermost of four Stars in a Zigzag line, north and south.

4th. Spica; a small white sparkling Star about 54° southeastward from Regulus.

5th. ANTARES; a large Red Star about 46° southeastward from Spica, having several small Stars westward of it like a Bow.

6th. β CAPRICORNI; is a small Star about 56° eastward from Antares, and known by another small Star near it northward,

4. The Stars without the Zodiac that are used in the Lunar Method, are introduced to supply the Defect of β Capricorni; namely,

7th. α PEGASI. 8th. α ARIETIS. 9th. α AQUILÆ, a white sparkling Star about 25° northward from β Capricorni, having a small Star near it northward. 10th. FOMALHAUT, a large Star about 45° south from α Pegasi.

5. The Zodiacal Stars that can most easily be found; are, Aldebaran, Pollux, Regulus, Spica, Antares; and out of the Zodiac, Aquilæ and Fomalhaut; the other three, α Pegasi, α Arietis and β Capricorni, are easily found by the Chart of Zodiacal Stars.

SECTION XXI.

Of the Positions which the Ecliptic and Zodiac may have, at different Times and Places.

Whilst the Celestial Bodies are apparently moving round the Earth's Axis from East toward West, and the Circles of the Celestial

32 Of the PHASES of the MOON.

lestial Sphere with them; the Ecliptic will take various Positions to the Horizon, during the Interval of every 24 Hours of Time.

The Moon and Zodiacal Stars being near the Ecliptic, their Positions to the Horizon, and to one another, must undergo the same Changes as the Circles of the Sphere, in which they are apparently situated.

1. In Latitude $66^{\circ} 32' N.$ when the Sun enters Capricorn; at Noon the Ecliptic and Horizon coincide. In the same Latitude South, when the Sun enters Cancer; at Noon the Ecliptic is in the Horizon.

2. At all other Places and Times; one Half of the Ecliptic is above the Horizon and the other half under it.

3. The Point of the Ecliptic in which the Sun apparently is, comes to the Meridian, likewise to the Horizon at Sun-rising and Sun-setting, with the Sun.

4. That Half of the Ecliptic which is above the Horizon, is changing its Position continually; sometimes it is perpendicular to the Horizon at some places, and at other times it is inclining to it northward or southward.

5. To Observers between the Tropics (that is, between $23^{\circ} 28'$ North and South Latitudes) the Ecliptic is Perpendicular to the the Horizon, once eastward and once westward in the Space of every 24 Hours.

6. The Fixed Stars without the Zodiac, become perpendicularly over or under the Moon frequently, according to their respective Places in the Heavens.

SECTION XXII.

Of the Cusps and Phases of the Moon, with their Positions to the Sun and Zodiacal Stars.

In order to understand how the Moon's Cusps or Phases are formed, it is necessary to know how she is illuminated by the Sun, and how she gets into North or South Latitude by crossing the Ecliptic under an Angle of $5^{\circ} 18'$ nearly.

Could the Moon be always accurately in the Ecliptic Line, the Line joining her Cusps, would be accurately at Right Angles to the Ecliptic; but as that cannot be, that Angle becomes varied according to her Latitude and Distance from the Sun.

This Method of finding the Zodiacal Stars by their Positions to the Moon and the Line joining her Cusps, is fully treated of in the *Theory and Practice of Longitude at Sea*, and the Use of the Chart of Zodiacal Stars.

Page 4. Ex. I. for $16''$ read $16'$

Page 9. Ex. I. for 24 feet read $32\frac{1}{2}$ feet.

Page 9. Ex. II. for 140 feet read $25\frac{1}{2}$ feet.

P. 10. line 2. for Table read Tables.

P. 13. line 23. for Log. read Degrees.

P. 15. line 18. for Sun read Star.

T H E E N D.